



Andreas Holzinger
VO 709.049 Medical Informatics
25.11.2015 11:15-12:45

Lecture 07

Knowledge, Decision, Uncertainty,
Bayesian Statistics, Probabilistic Modelling

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<http://hci-kdd.org/biomedical-informatics-big-data>



- 1. Intro: Computer Science meets Life Sciences, challenges, future directions
- 2. Back to the future: Fundamentals of Data, Information and Knowledge
- 3. Structured Data: Coding, Classification (ICD, SNOMED, MeSH, UMLS)
- 4. Biomedical Databases: Acquisition, Storage, Information Retrieval and Use
- 5. Semi structured and weakly structured data (structural homologues)
- 6. Multimedia Data Mining and Knowledge Discovery
- **7. Knowledge, Decision, Cognition, Probability, Uncertainty, Bayes & Co**
- 8. Biomedical Decision Making: Reasoning and Decision Support
- 9. Intelligent Information Visualization and Visual Analytics
- 10. Biomedical Information Systems and Medical Knowledge Management
- 11. Biomedical Data: Privacy, Safety and Security
- 12. Methodology for Info Systems: System Design, Usability & Evaluation

- Bayes theorem
- Case based reasoning
- Differential diagnosis
- Human decision making
- Hypothetico-deductive method
- Incomplete data
- Model of human information processing
- Modeling patient health
- PDCA-Deming wheel
- Receiver operating characteristics
- Rough set theory
- Selected attention
- Signal detection theory
- Triage

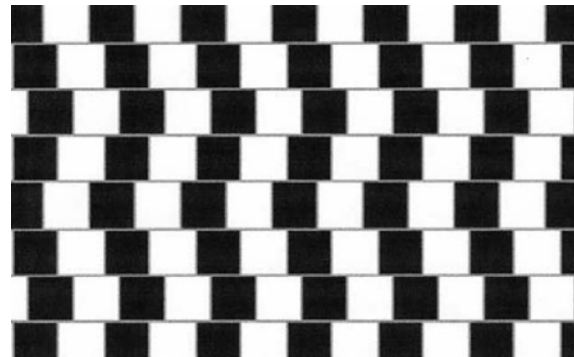
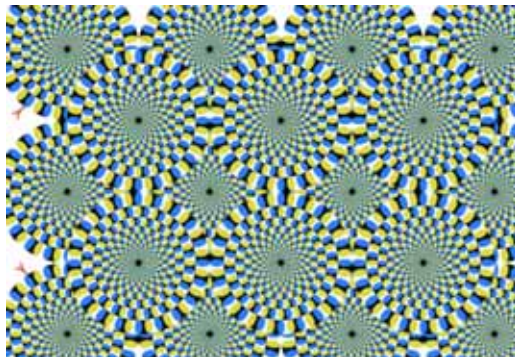
- **Brute Force** = a trivial very general problem-solving technique that consists of systematically enumerating all possible candidates for the solution and checking whether each candidate satisfies the problem's statement;
- **Cognition** = mental processes of gaining knowledge, comprehension, including thinking, attention, remembering, language understanding, decision making and problem-solving;
- **Cognitive load** = According to Sweller (1996) a measure of complexity and difficulty of a task, related to the executive control of the short-term memory, correlating with factors including (human) performance; based on the chunk-theory of Miller (1956);
- **Cognitive Science** = interdisciplinary study of human information processing, including perception, language, memory, reasoning, and emotion;
- **Confounding Variable** = an unforeseen, unwanted variable that jeopardizes reliability and validity of a study outcome.
- **Correlation coefficient** = measures the relationship between pairs of interval variables in a sample, from $r = -1.00$ to 0 (no correlation) to $r = +1.00$
- **Decision Making** = a central cognitive process in every medical activity, resulting in the selection of a final choice of action out of alternatives; according to Shortliffe (2011) DM is still the key topic in medical informatics;
- **Diagnosis** = classification of a patient's condition into separate and distinct categories that allow medical decisions about treatment and prognostic;
- **Differential Diagnosis (DDx)** = a systematic method to identify the presence of an entity where multiple alternatives are possible, and the process of elimination, or interpretation of the probabilities of conditions to negligible levels;
- **Evidence-based medicine (EBM)** = aiming at the best available evidence gained from the scientific method to clinical decision making. It seeks to assess the strength of evidence of the risks and benefits of treatments (including lack of treatment) and diagnostic tests. Evidence quality can range from meta-analyses and systematic reviews of double-blind, placebo-controlled clinical trials at the top end, down to conventional wisdom at the bottom;

- **External Validity** = the extent to which the results of a study are generalizable or transferable;
- **Hypothetico-Deductive Model (HDM)** = formulating a hypothesis in a form that could conceivably be falsified by a test on observable data, e.g. a test which shows results contrary to the prediction of the hypothesis is the falsification, a test that could but is not contrary to the hypothesis corroborates the theory – then you need to compare the explanatory value of competing hypotheses by testing how strong they are supported by their predictions;
- **Internal Validity** = the rigor with which a study was conducted (e.g., the design, the care taken to conduct measurements, and decisions concerning what was and was not measured);
- **PDCA** = Plan-Do-Check-Act, The so called PDCA-cycle or Deming-wheel can be used to coordinate a systematic and continuous improvement. Every improvement starts with a goal and with a plan on how to achieve that goal, followed by action, measurement and comparison of the gained output.
- **Perception** = sensory experience of the world, involving the recognition of environmental stimuli and actions in response to these stimuli;
- **Qualitative Research** = empirical research exploring relationships using textual, rather than quantitative data, e.g. case study, observation, ethnography; Results are not considered generalizable, but sometimes at least transferable.
- **Quantitative Research** = empirical research exploring relationships using numeric data, e.g. surveys, quasi-experiments, experiments. Results should be generalized, although it is not always possible.
- **Reasoning** = cognitive (thought) processes involved in making medical decisions (clinical reasoning, medical problem solving, diagnostic reasoning, behind every action);
- **Receiver-operating characteristic (ROC)** = in signal detection theory this is a graphical plot of the sensitivity, or true positive rate, vs. false positive rate ($1 - \text{specificity}$ or $1 - \text{true negative rate}$), for a binary classifier system as its discrimination threshold is varied;
- **Symbolic reasoning** = logical deduction
- **Triage** = process of judging the priority of patients' treatments based on the severity of their condition;

- CES = Central Executive System
- DDx = Differential Diagnosis
- DM = Decision Making
- DSS = Decision Support System
- EBM = Evidence-based medicine
- fMRI = functional Magnetic Resonance Image
- HDM = Hypothetico-Deductive Model
- IOM = Institute of Medicine
- LTS = Long Term Storage
- ME = Medical Error
- PDCA = Plan-Do-Check-Act
- QM = Quality Management
- ROC = Receiver Operating Characteristic
- ROC = Receiver-operating characteristic
- RST = Rough Set Theory
- STS = Short Term Storage
- USTS = Ultra Short Term Storage

- ... are familiar with some principles and elements of human information processing;
- ... can discriminate between perception, cognition, thinking, reasoning & problem solving;
- ... have got insight into some basics of human decision making processes;
- ... got an overview of the Hypothetico-Deductive Method HDM versus PCDA Deming approach;
- ... have acquired some basics on modeling patient health, differential diagnosis, case-based reasoning and medical errors;

- Time to make a decision = “5 Minutes” [1], [2]
- Limited perceptual, attentive and cognitive human resources [3], and Human error
- Noisy, missing, probabilistic, uncertain data



- [1] Gigerenzer, G. 2008. *Gut Feelings: Short Cuts to Better Decision Making* London, Penguin.
- [2] Gigerenzer, G. & Gaissmaier, W. 2011. Heuristic Decision Making. In: Fiske, S. T., Schacter, D. L. & Taylor, S. E. (eds.) *Annual Review of Psychology*, Vol 62. pp. 451-482.
- [3] Bialek, W. 1987. Physical Limits to Sensation and Perception. *Annual Review of Biophysics and Biophysical Chemistry*, 16, 455-478.

Medical Diagnosis - Decision Making

Slide 7-2: Decision Making is central in Biomedical Informatics



Source: Cisco (2008).
Cisco Health Presence
Trial at Aberdeen Royal
Infirmary in Scotland

3 July 1959, Volume 130, Number 3366

SCIENCE

Reasoning Foundations of Medical Diagnosis

Symbolic logic, probability, and value theory
aid our understanding of how physicians reason.

Robert S. Ledley and Lee B. Lusted

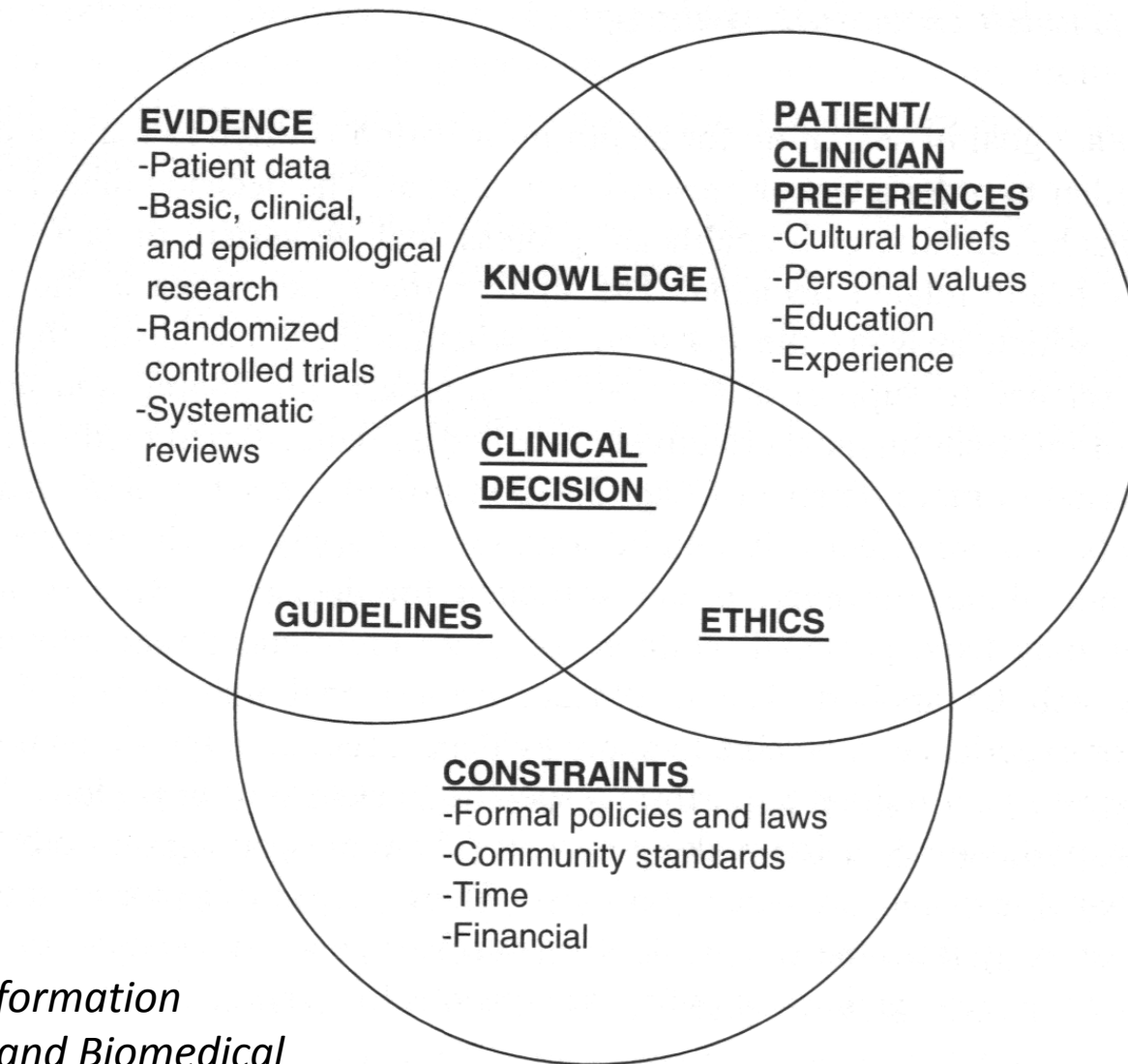
The purpose of this article is to analyze the complicated reasoning processes inherent in medical diagnosis. The importance of this problem has received recent emphasis by the increasing interest in the use of electronic computers as an aid to medical diagnostic processes

fitted into a definite disease category, or that it may be one of several possible diseases, or else that its exact nature cannot be determined." This, obviously, is a greatly simplified explanation of the process of diagnosis, for the physician might also comment that after seeing a

ance are the ones who do remember and consider the most possibilities."

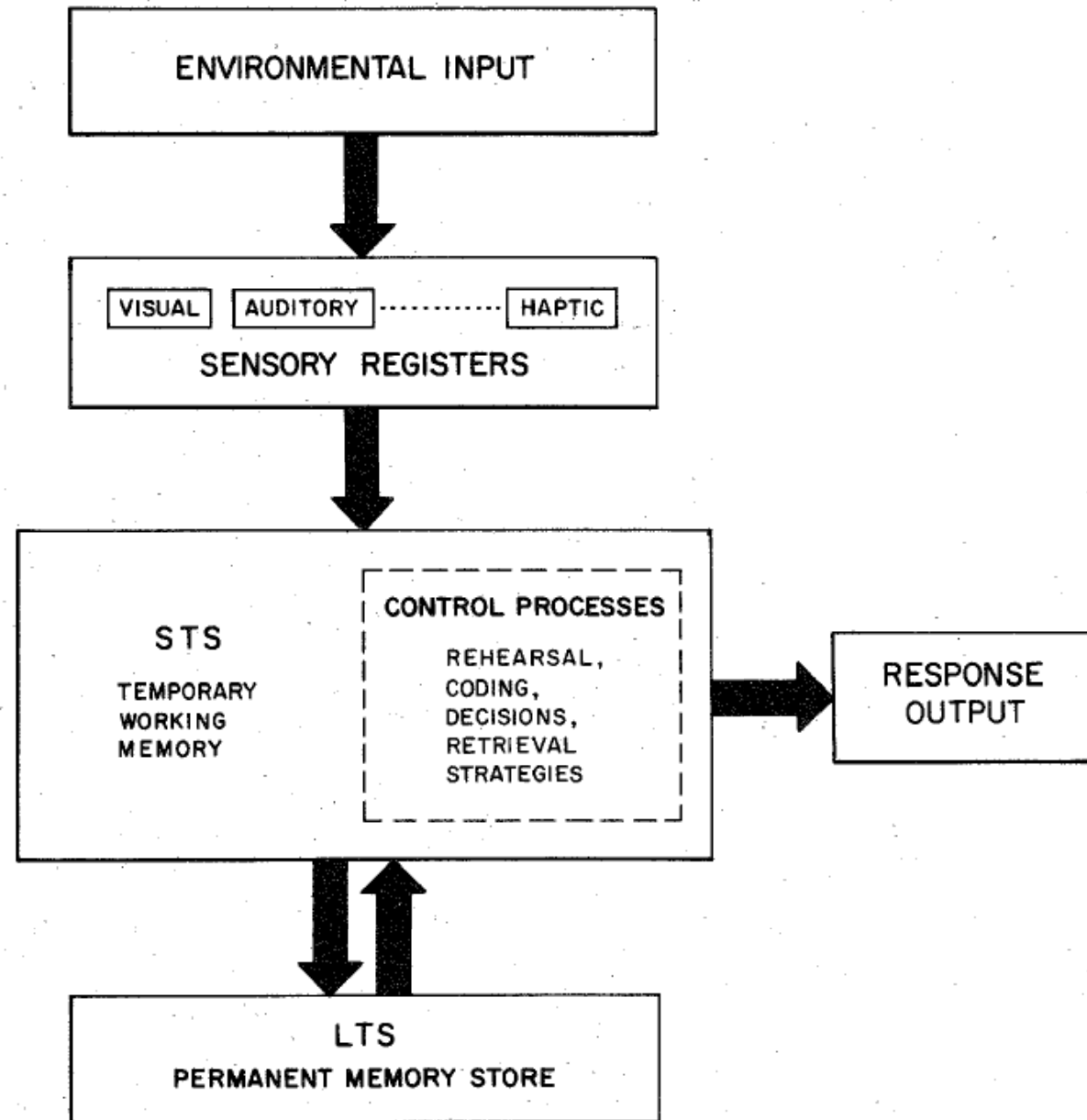
Computers are especially suited to help the physician collect and process clinical information and remind him of diagnoses which he may have overlooked. In many cases computers may be as simple as a set of hand-sorted cards, whereas in other cases the use of a large-scale digital electronic computer may be indicated. There are other ways in which computers may serve the physician, and some of these are suggested in this paper. For example, medical students might find the computer an important aid in learning the methods of differential diagnosis. But to use the computer thus we must understand how the physician makes a medical diagnosis. This, then, brings us to the subject of our investigation: the reasoning foundations of medical diagnosis and treatment.

Medical diagnosis involves processes that can be systematically analyzed, as well as those characterized as "intangible." For instance, the reasoning foundations of medical diagnostic procedures

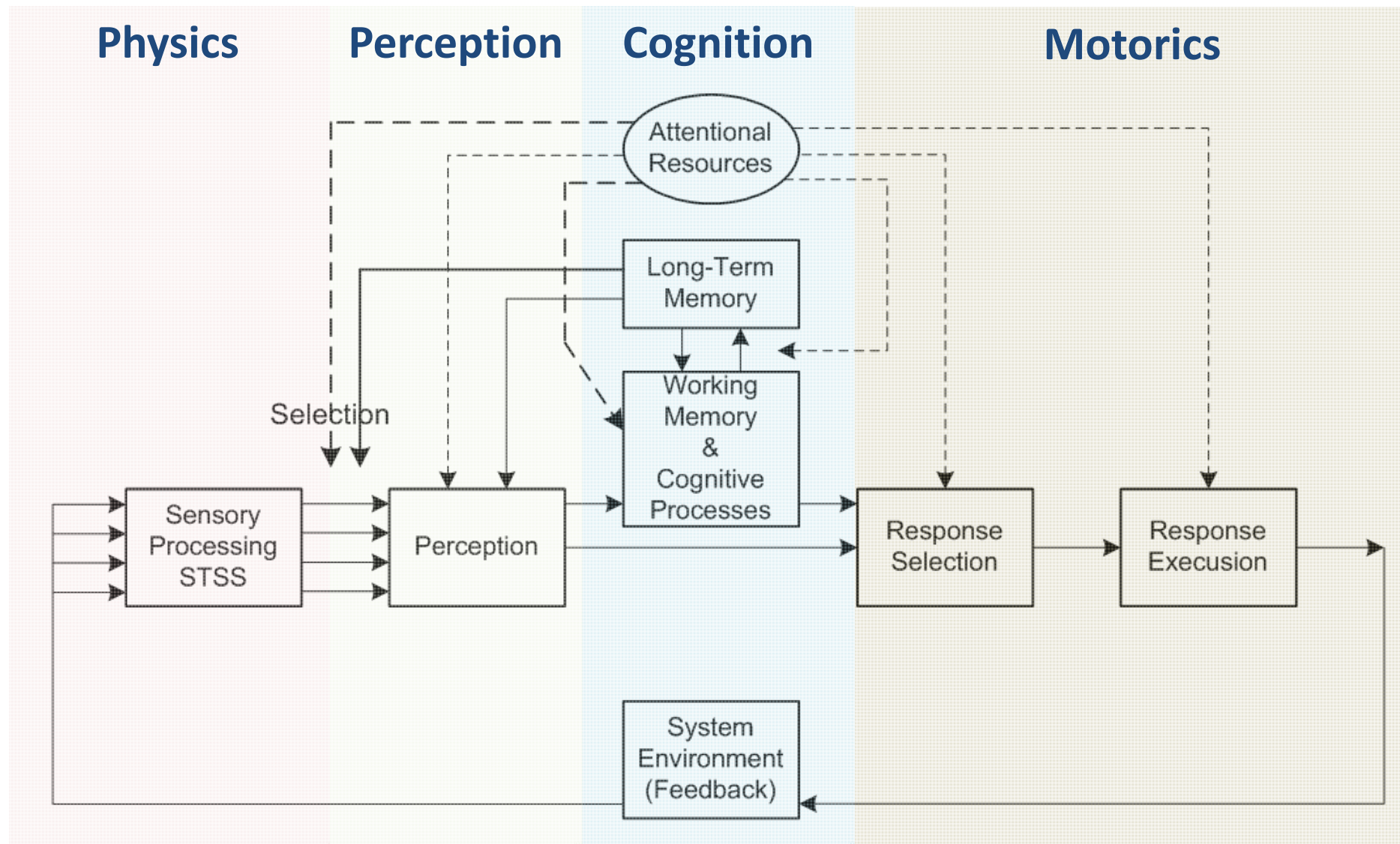


Hersh, W. (2010) *Information Retrieval: A Health and Biomedical Perspective*. New York, Springer.

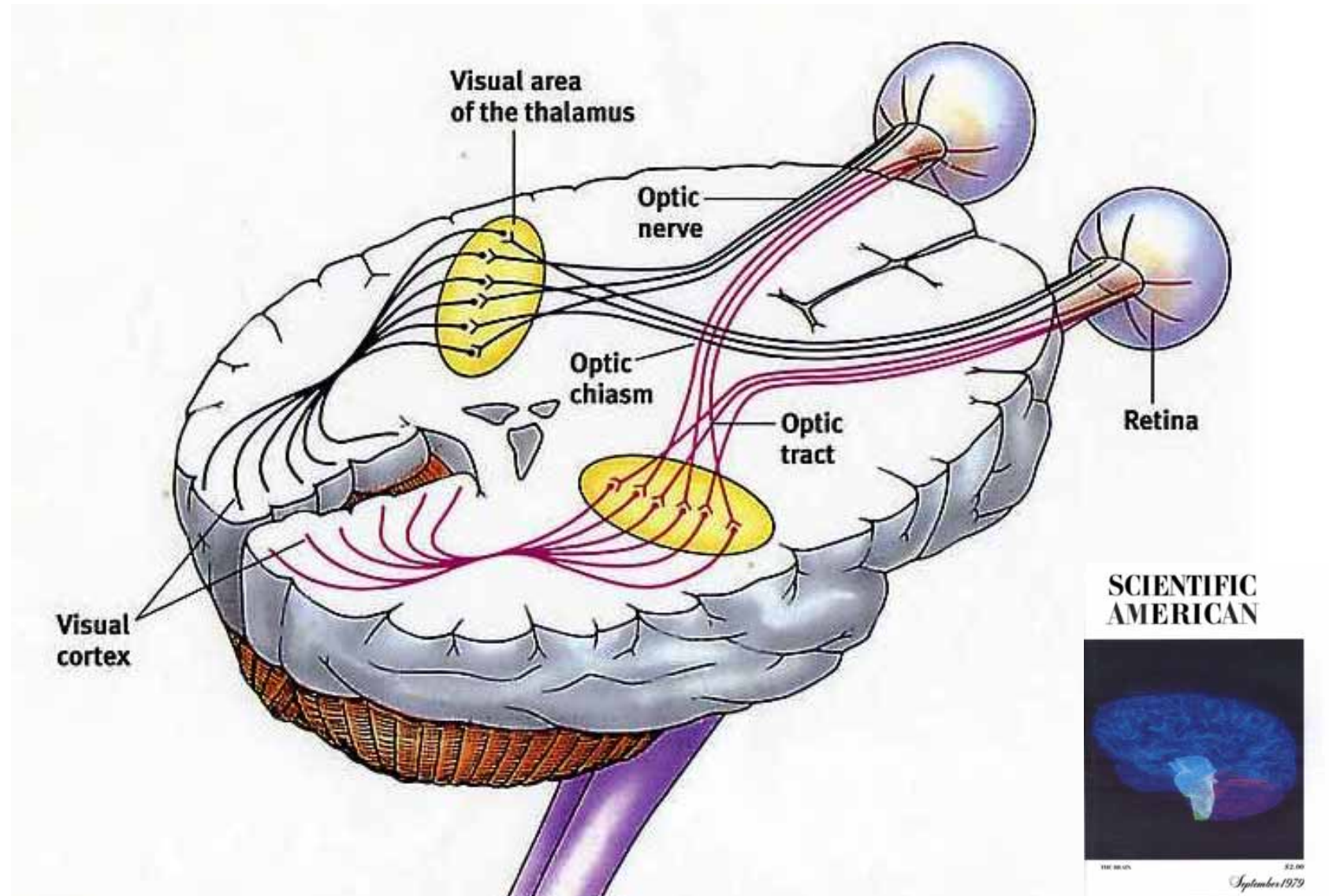
Human Information Processing



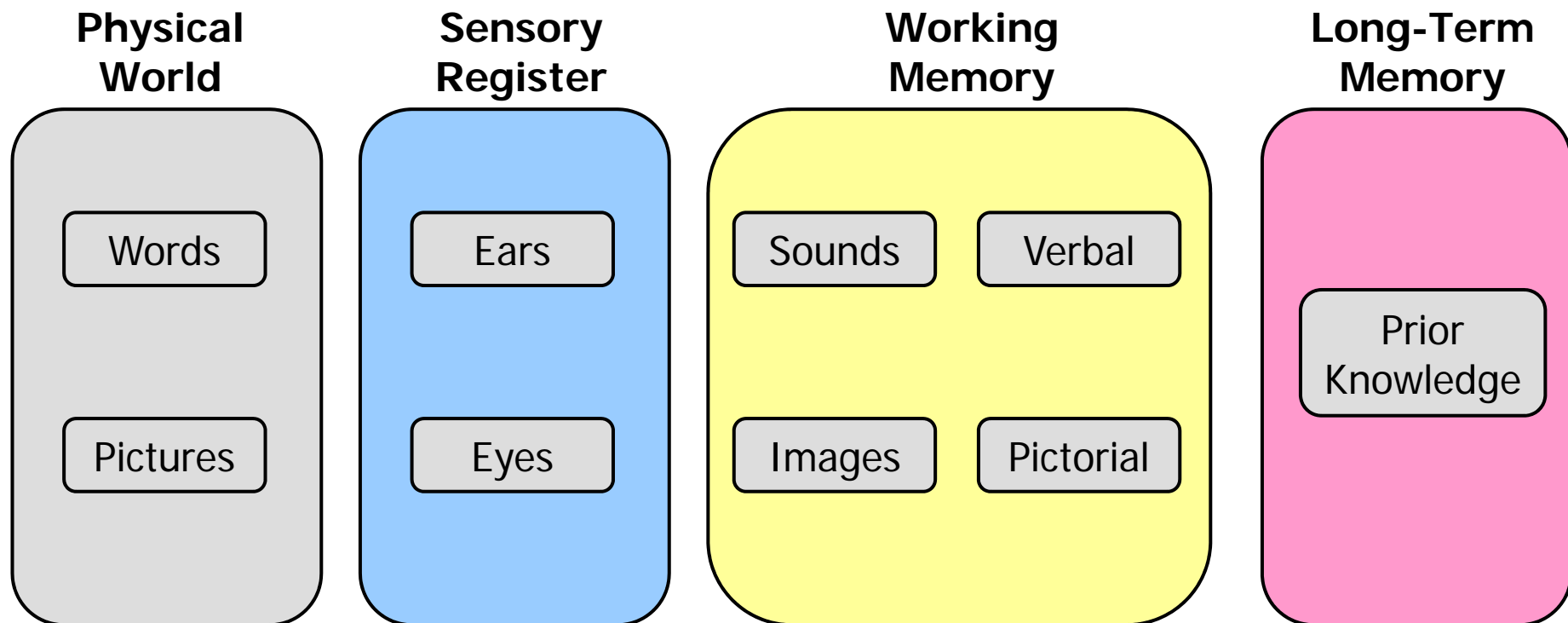
Atkinson, R. C. & Shiffrin, R. M. (1971) *The control processes of short-term memory* (Technical Report 173, April 19, 1971). Stanford, Institute for Mathematical Studies in the Social Sciences, Stanford University.



Wickens, C., Lee, J., Liu, Y. & Gordon-Becker, S. (2004) *Introduction to Human Factors Engineering: Second Edition*. Upper Saddle River (NJ), Prentice-Hall.

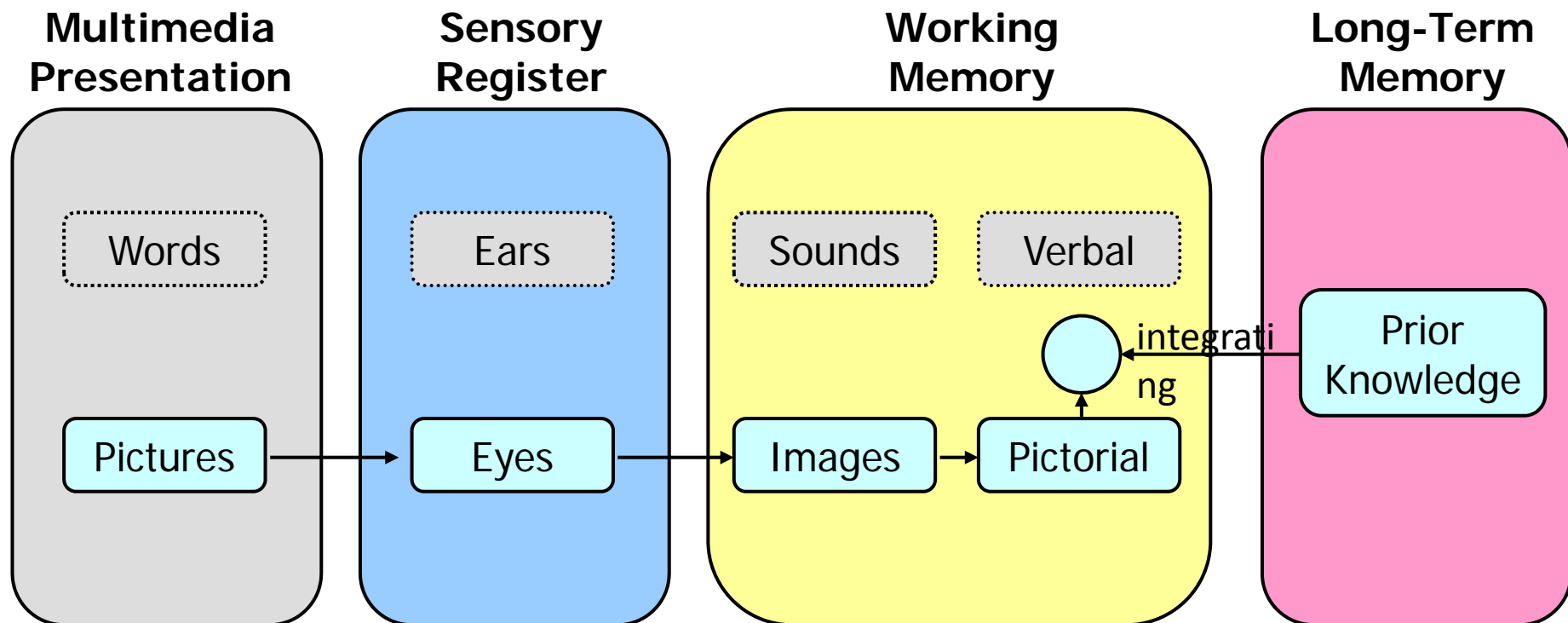


Source: Department of Neuroscience, The Mount Sinai School of Medicine (2004)



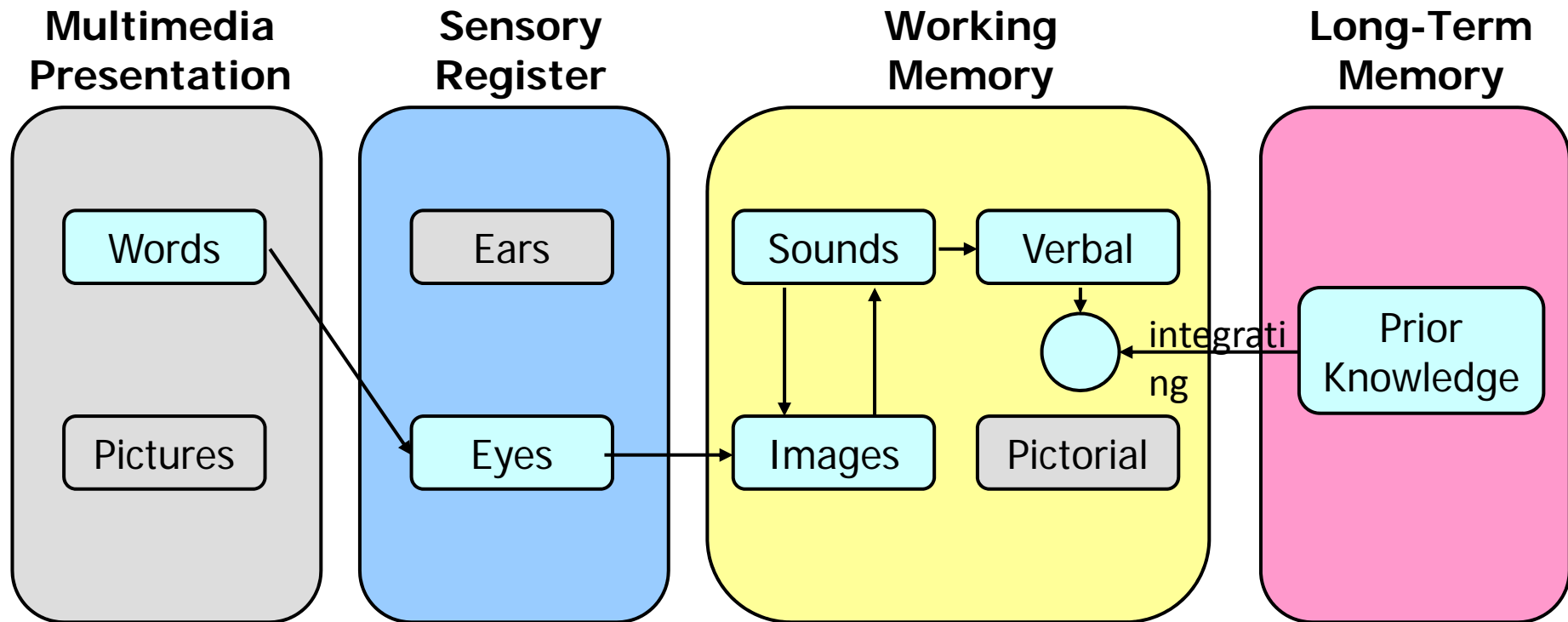
cf. with Paivio (1973), Mayer & Moreno (1998), Holzinger (2000), Schnotz & Bannert (2002)

a) Processing of visual information (PICTURES)



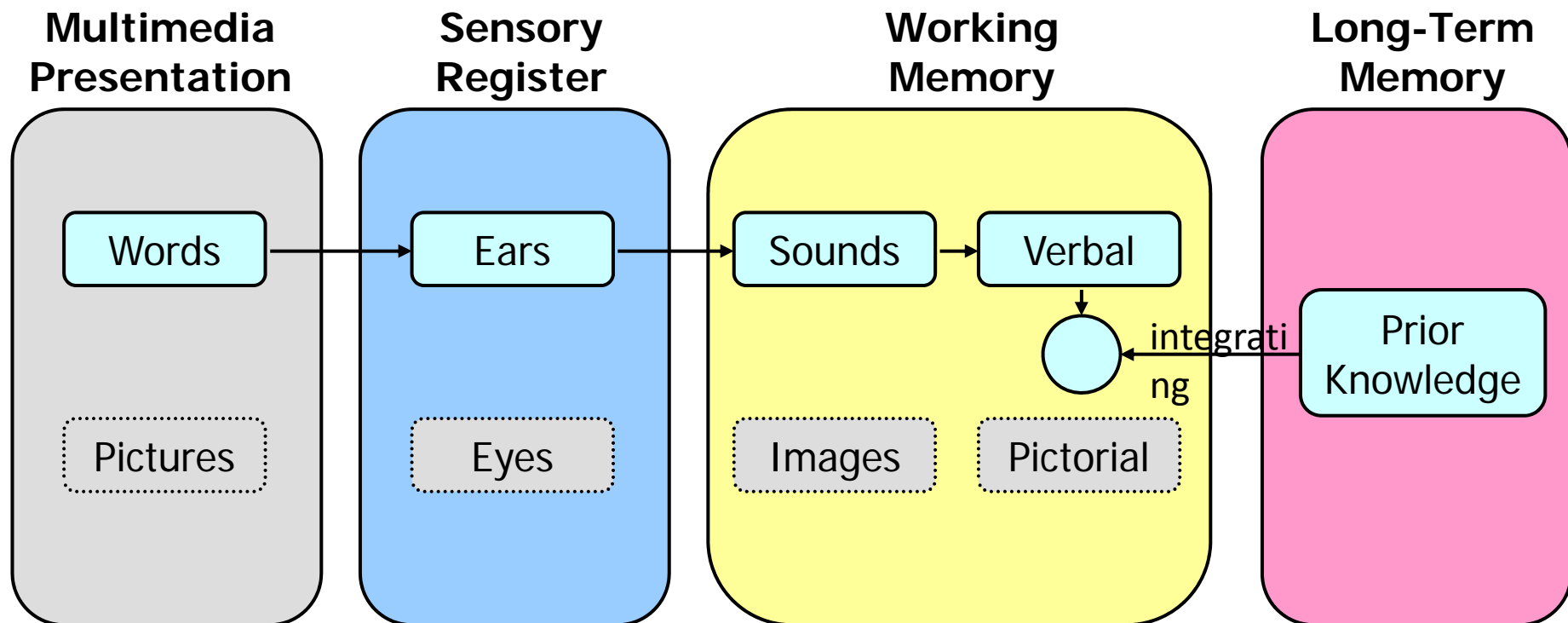
cf. with Paivio (1973), Mayer & Moreno (1998), Holzinger (2000), Schnotz & Bannert (2002)

b) Processing of visual information (PRINTED WORDS)

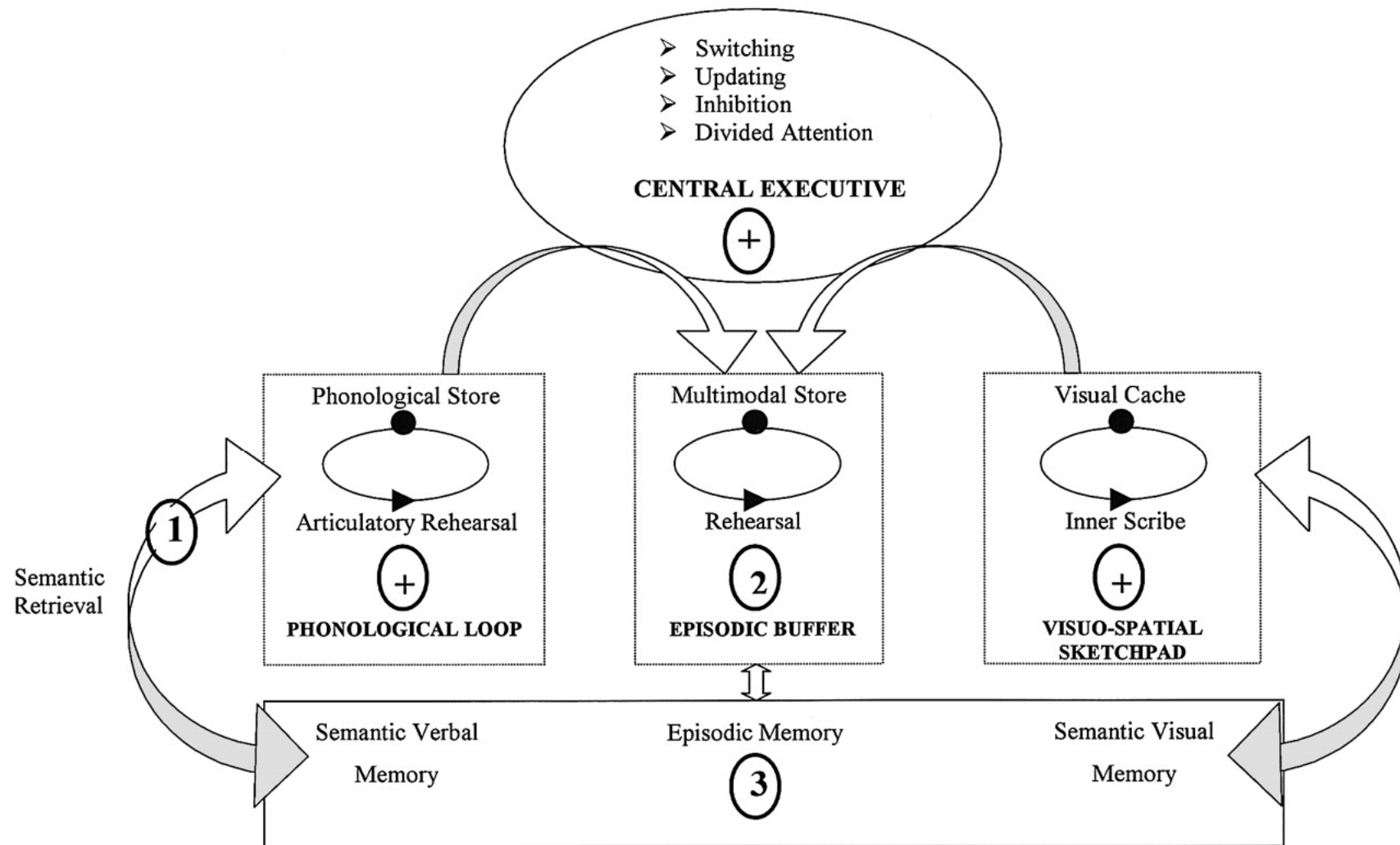


cf. with Paivio (1973), Mayer & Moreno (1998), Holzinger (2000), Schnotz & Bannert (2002)

c) Processing of audio information (SPOKEN WORDS)

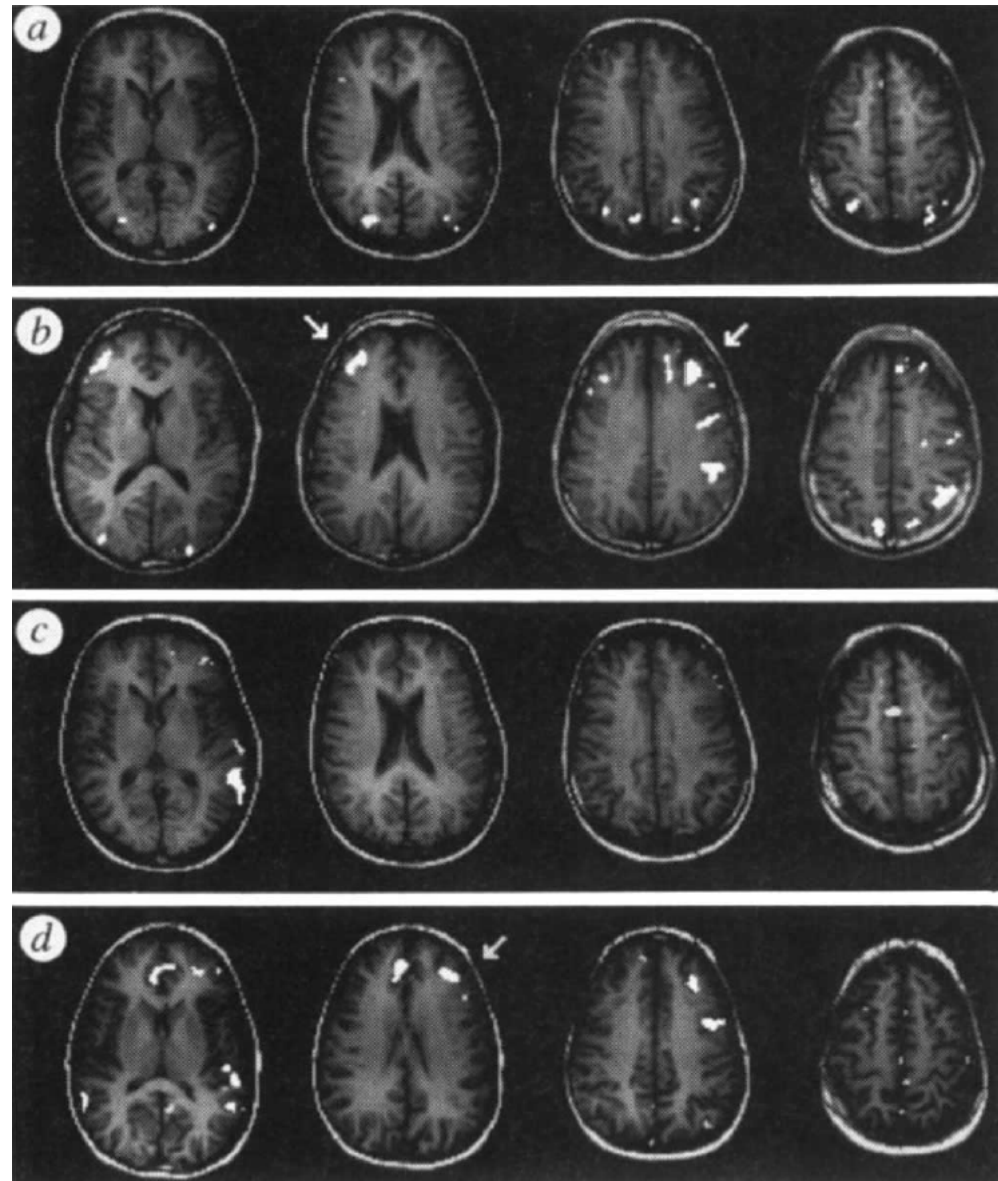


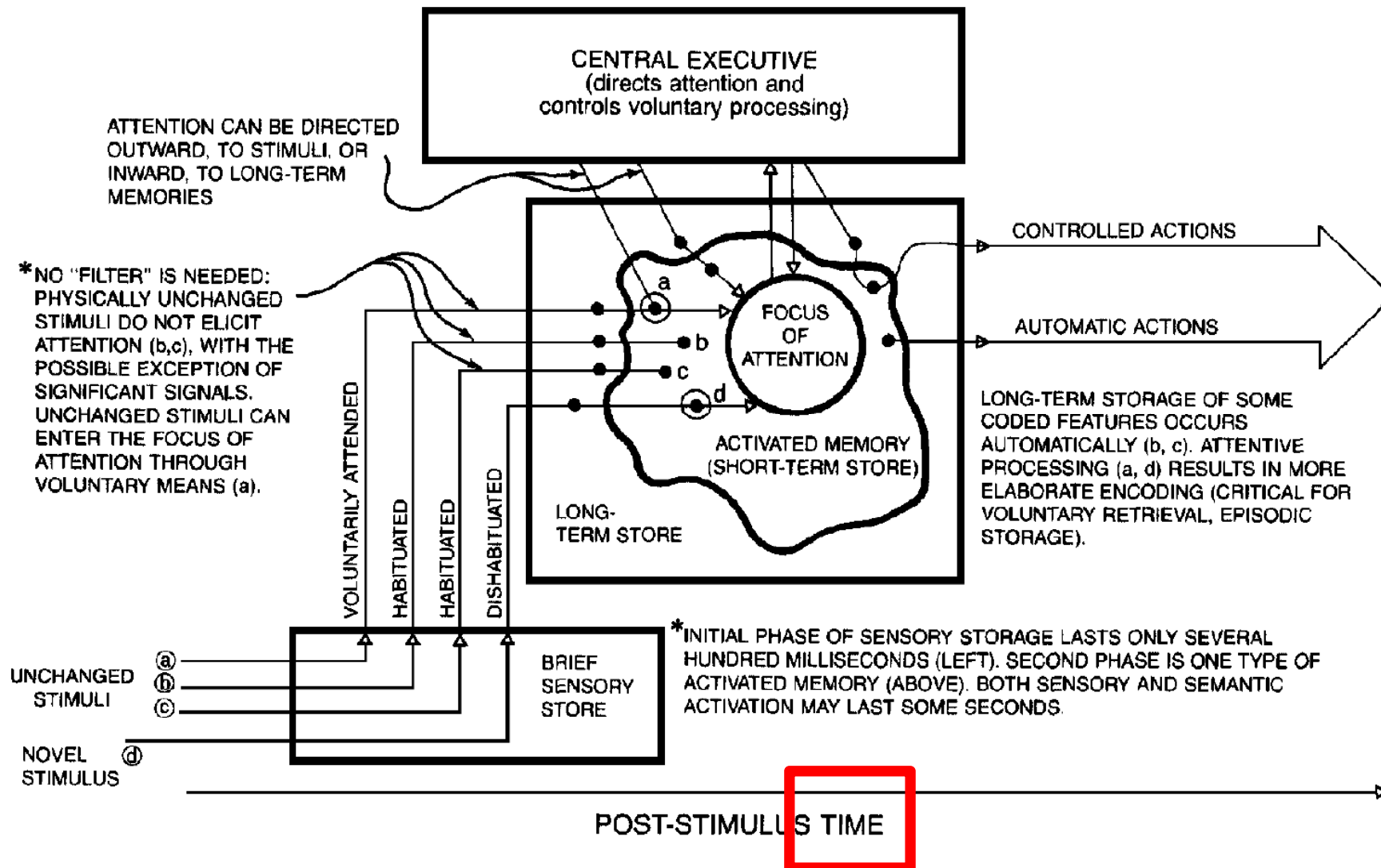
cf. with Paivio (1973), Mayer & Moreno (1998), Holzinger (2000), Schnotz & Bannert (2002)



Quinette, P., Guillery, B., Desgranges, B., de la Sayette, V., Viader, F. & Eustache, F. (2003)
Working memory and executive functions in transient global amnesia. *Brain*, 126, 9, 1917-1934.

D'Esposito, M., Detre, J. A., Alsop, D. C., Shin, R. K., Atlas, S. & Grossman, M. (1995) The neural basis of the central executive system of working memory. *Nature*, 378, 6554, 279-281.

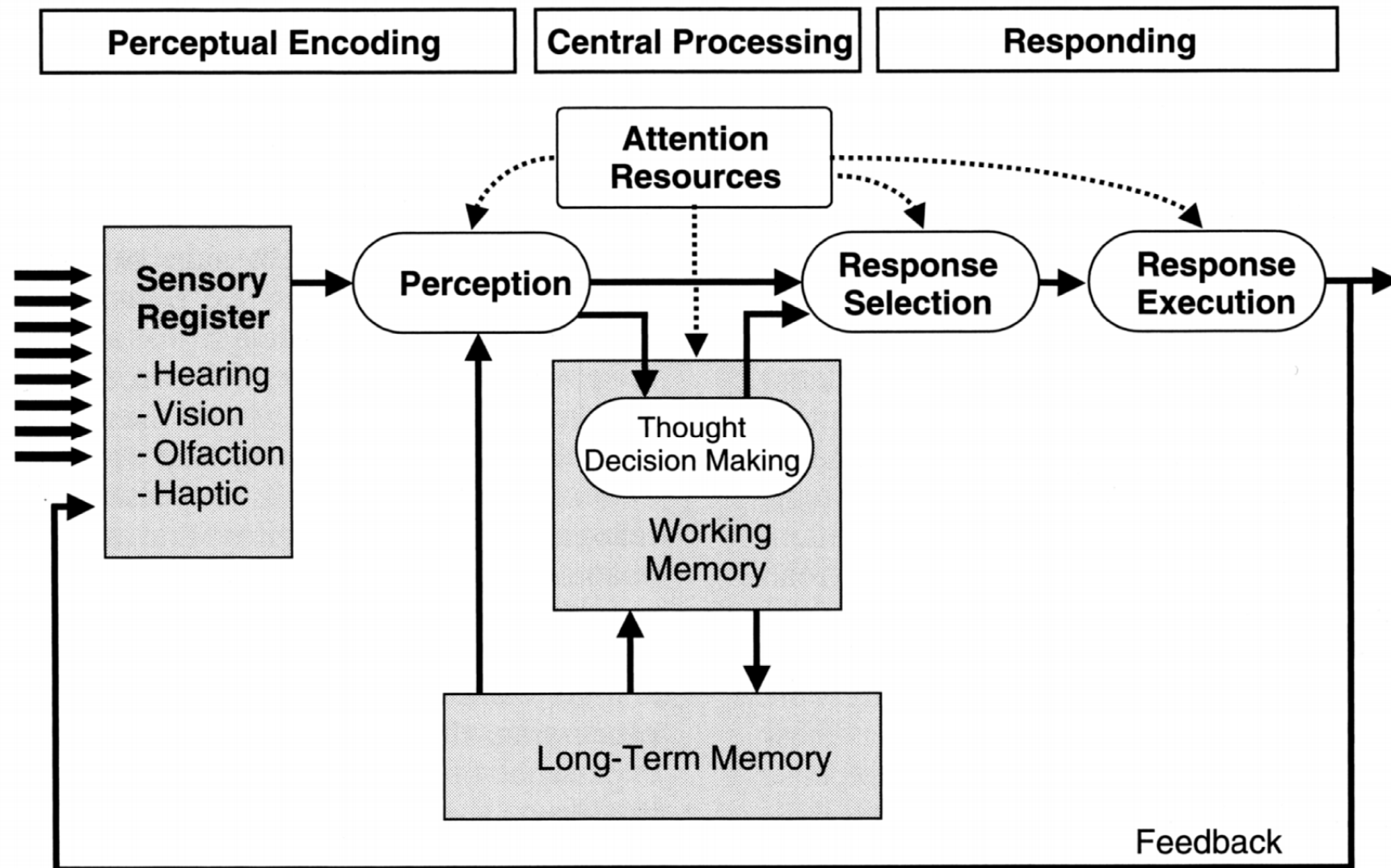




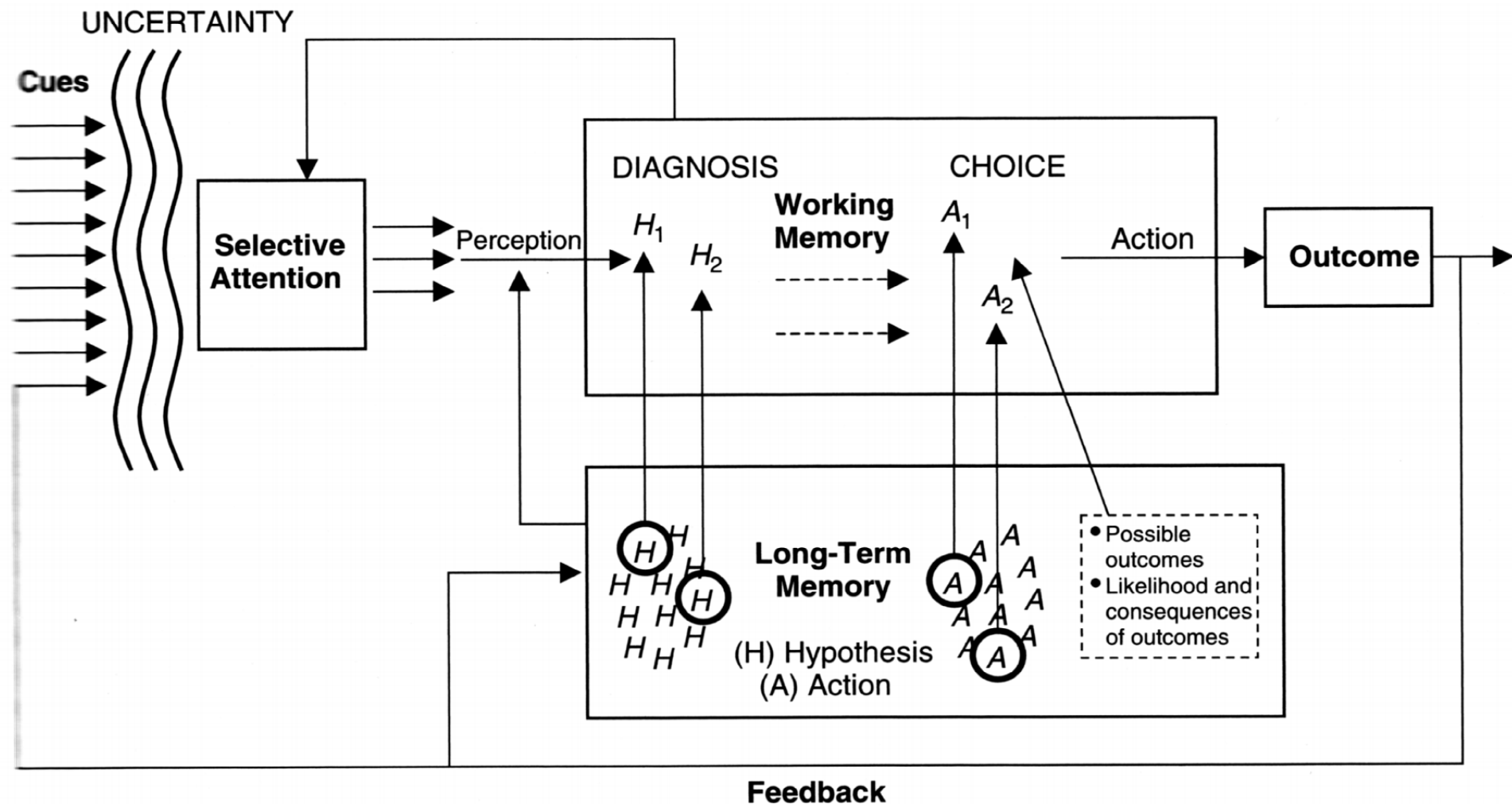
Cowan, N. (1988) Evolving conceptions of memory storage, selective attention, and their mutual constraints within the human information-processing system. *Psychological Bulletin*, 104, 2, 163.



Simons, D. J. & Chabris, C. F. 1999. Gorillas in our midst: sustained inattention blindness for dynamic events. *Perception*, 28, (9), 1059-1074.



Wickens, C. D. (1984) *Engineering psychology and human performance*. Columbus (OH), Charles Merrill.



Wickens, C. D. (1984) *Engineering psychology and human performance*. Columbus (OH), Charles Merrill.

Start with the most simplest decision support system

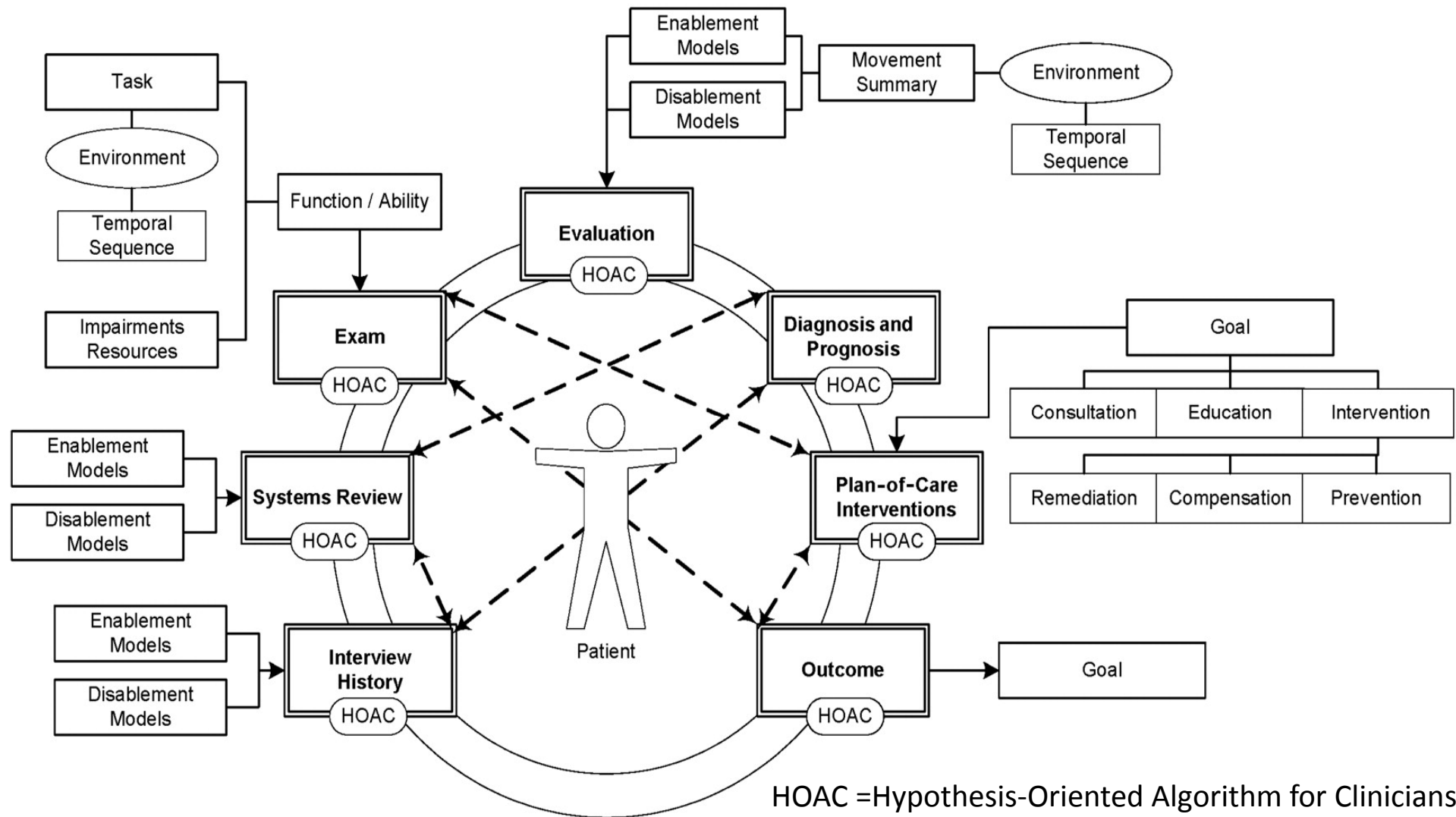


Iserson, K. V. & Moskop, J. C. 2007. Triage in Medicine, Part I: Concept, History, and Types. *Annals of Emergency Medicine*, 49, (3), 275-281.

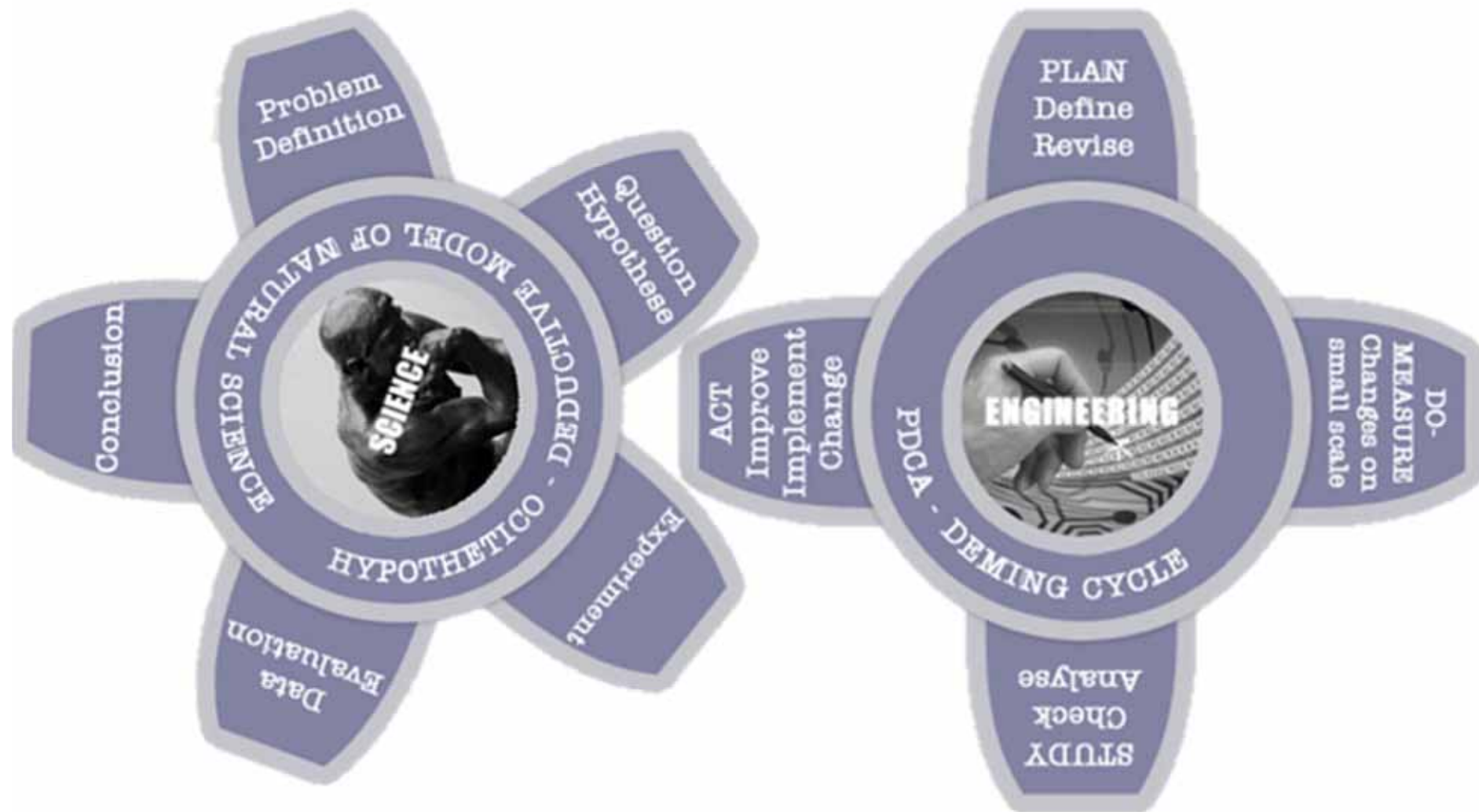
Nº 568989		Nº 568989 <small>EYES: Yellow EARS: Reddened</small>	
EYACU-AID™ TRIAGE TAG 		Nº 568989 CONTAMINATION: NO ___ YES ___ <small>(Under Eyes)</small>	
Respiration ___ fast ___ slow Pulse ___ < 5 SEC ___ ≥ 5 SEC			
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Time	Pulse	BP	Respiration
Time	Drug/Dosage	Diagnosis	
Major Injuries _____		Allergies _____	
Destination _____		Prescription Medication _____	
Personal Information			
Name _____		Address _____	
City _____ State _____ Zip _____ Phone _____		Male _____ Female _____ Age _____ Weight _____	

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Source: <http://store.gomed-tech.com>



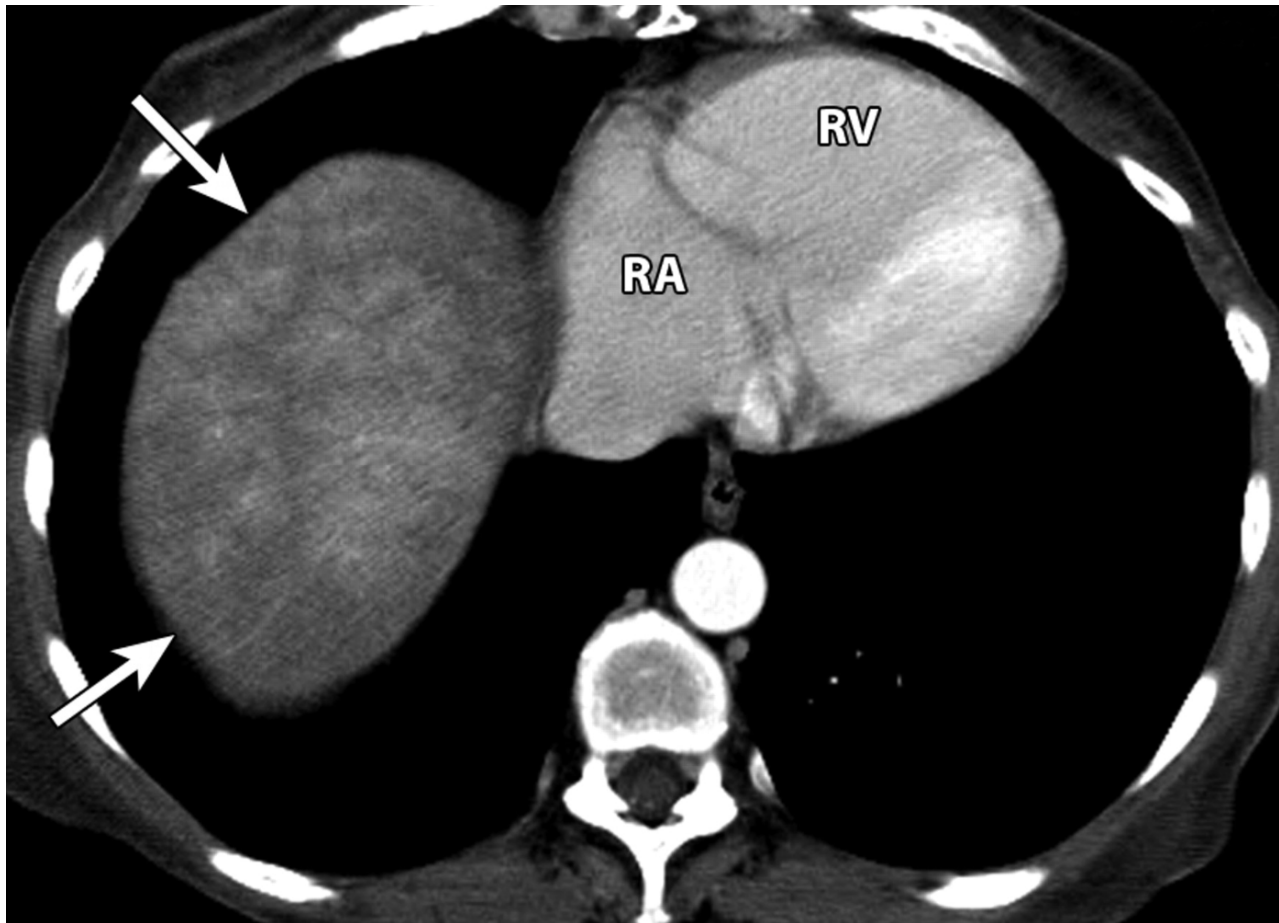
Schenkman, M., Deutsch, J. E. & Gill-Body, K. M. (2006) An Integrated Framework for Decision Making in Neurologic Physical Therapist Practice. *Physical Therapy*, 86, 12, 1681-1702.



Holzinger, A. (2010) *Process Guide for Students for Interdisciplinary Work in Computer Science/Informatics. Second Edition.* Norderstedt, BoD. Online: <http://www.hci4all.at>

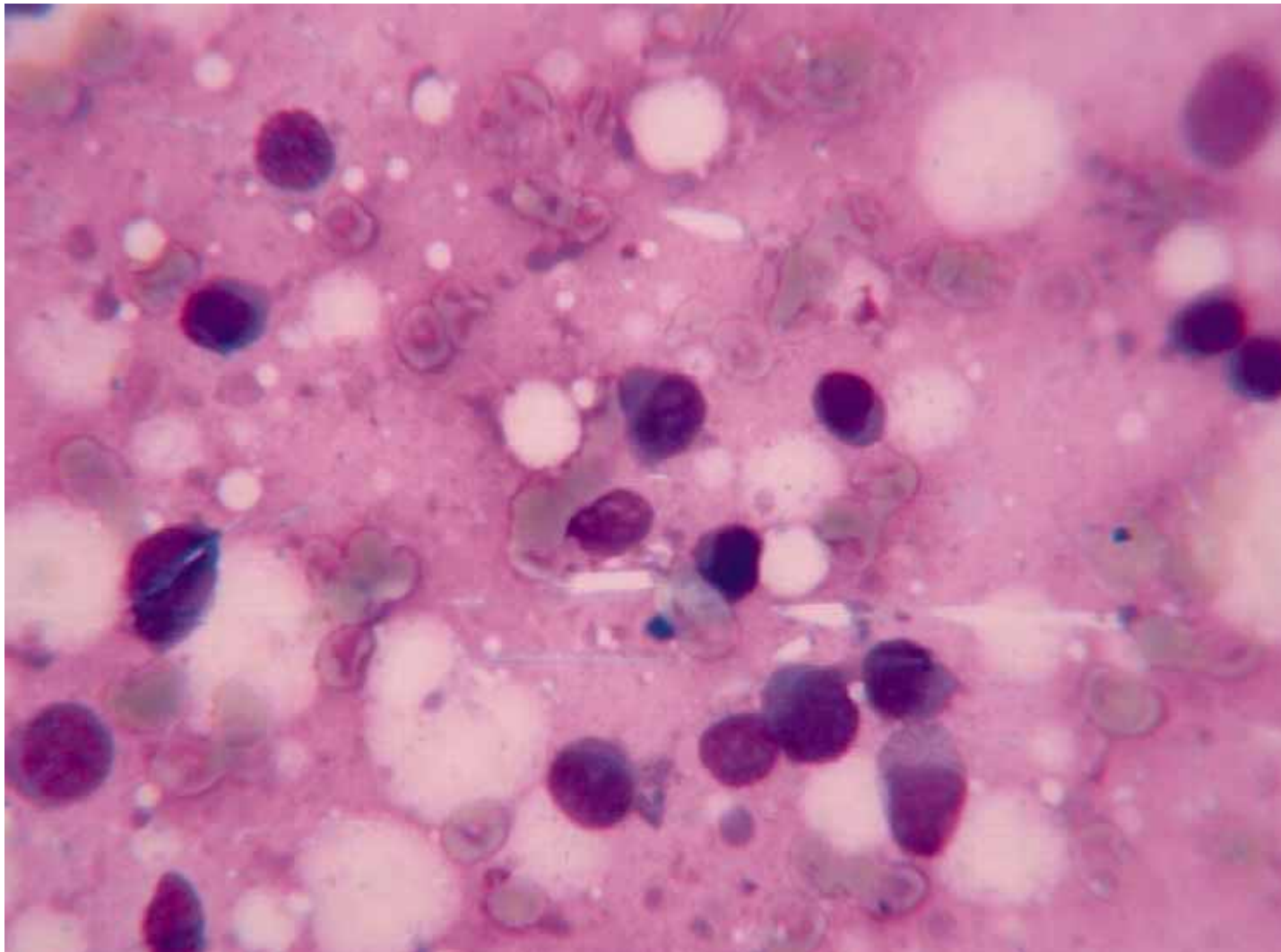
Example 1/4: carcinoid heart disease (chd)

Hepatic venous congestion and carcinoid heart disease secondary to an ovarian carcinoid tumor in a 56-year-old woman with elevated liver enzyme levels and right upper quadrant pain.



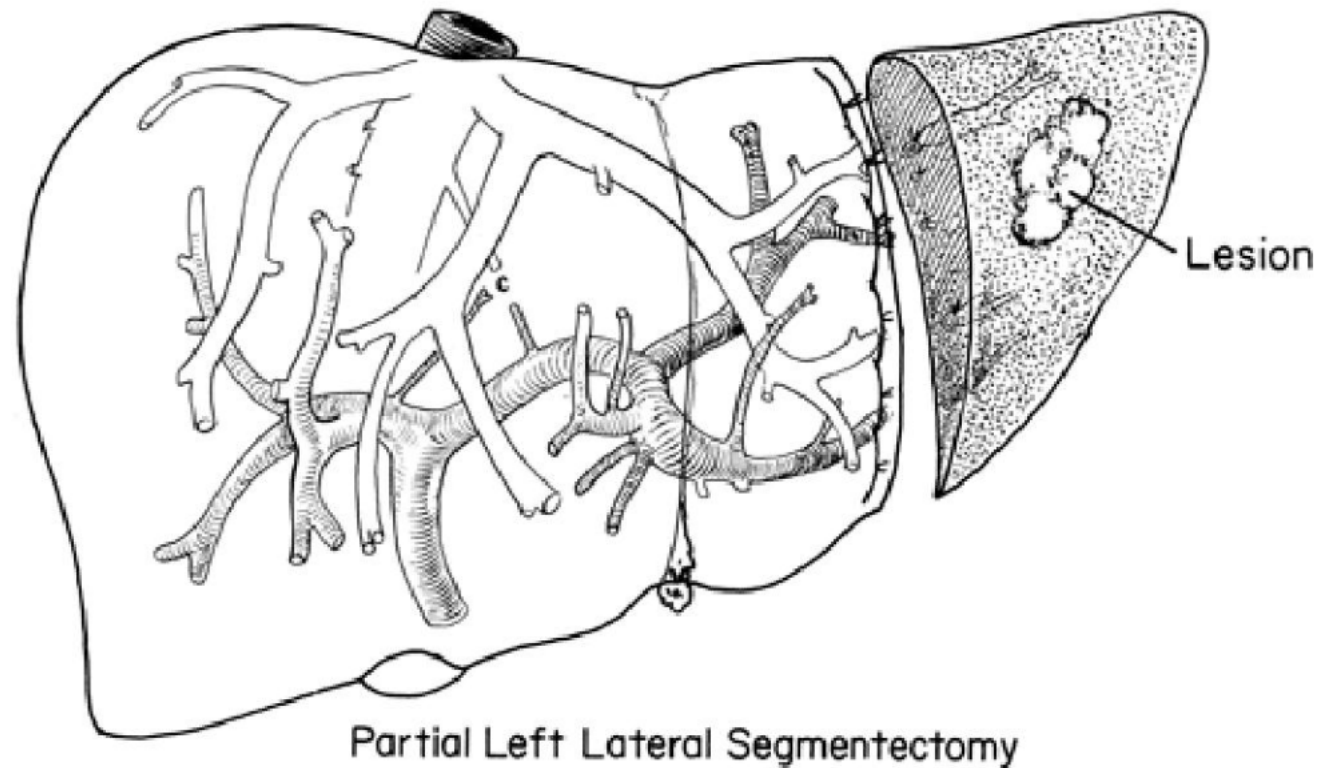
Shanbhogue, A. K. P., Shanbhogue, D. K. P., Prasad, S. R., Surabhi, V. R., Fasih, N. & Menias, C. O. (2010) Clinical Syndromes Associated with Ovarian Neoplasms: A Review. *Radiographics*, 30, 4, 903-919.

Example 2/4: bone-marrow depression (bmd)



Prasad, M., Maitra, A., Sethiya, N., Bharadwaj, V. K., Chowdhury, V., Valecha, J. & Biswas, R. (2009) Acute renal failure followed by low back ache. *BMJ Case Reports*, 2009.

Example 3/4: partial liver resection (plr)

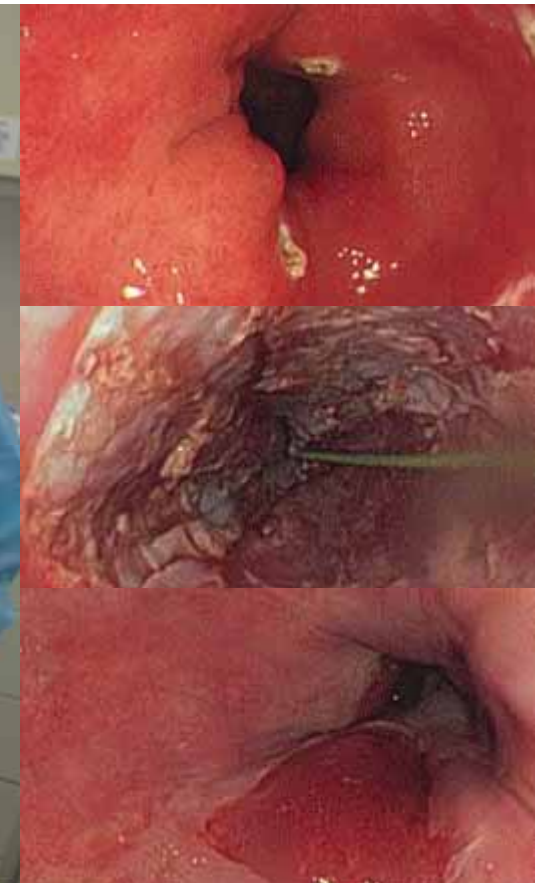


Zollinger, R. M. & Ellison, C. (2010) *Zollinger's Atlas of Surgical Operations (9th Edition)*. New York, McGraw Hill.

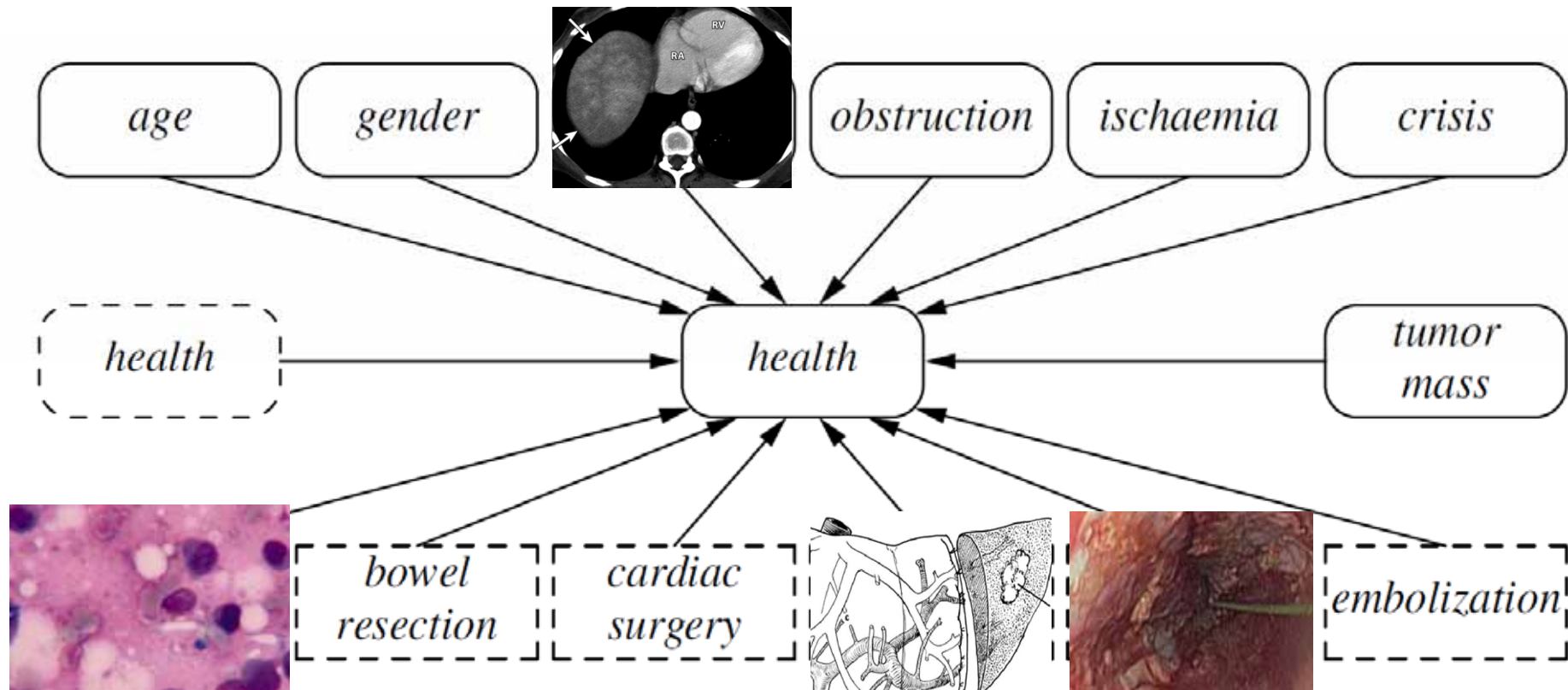
Example 4/4: radiofrequency ablation (rfa)



Holston Valley Medical Center



van Vilsteren, F. G. I. et al. (2011) Stepwise radical endoscopic resection versus radiofrequency ablation for Barrett's oesophagus with high-grade dysplasia or early cancer: a multicentre randomised trial. *GUT*.



chd = carcinoid heart disease; bmd = bone-marrow depression; plr = partial liver resection;
rfa = radiofrequency ablation; dashed ... past states; square objects ... treatments

van Gerven, M. A. J., Taal, B. G. & Lucas, P. J. F. (2008) Dynamic Bayesian networks as prognostic models for clinical patient management. *Journal of Biomedical Informatics*, 41, 4, 515-529.

Let $\mathbf{U} \subseteq \mathbf{X}$ denote this risk factors and
Let $\mathbf{V} = \mathbf{X} \setminus \mathbf{U}$ denote the complement.

The risk of immediate death $p(\text{health}(t) = \text{death} | \mathbf{X})$ can be expressed by calculation of the following product:

$$\prod_{U \in \mathbf{U}} p(U)$$

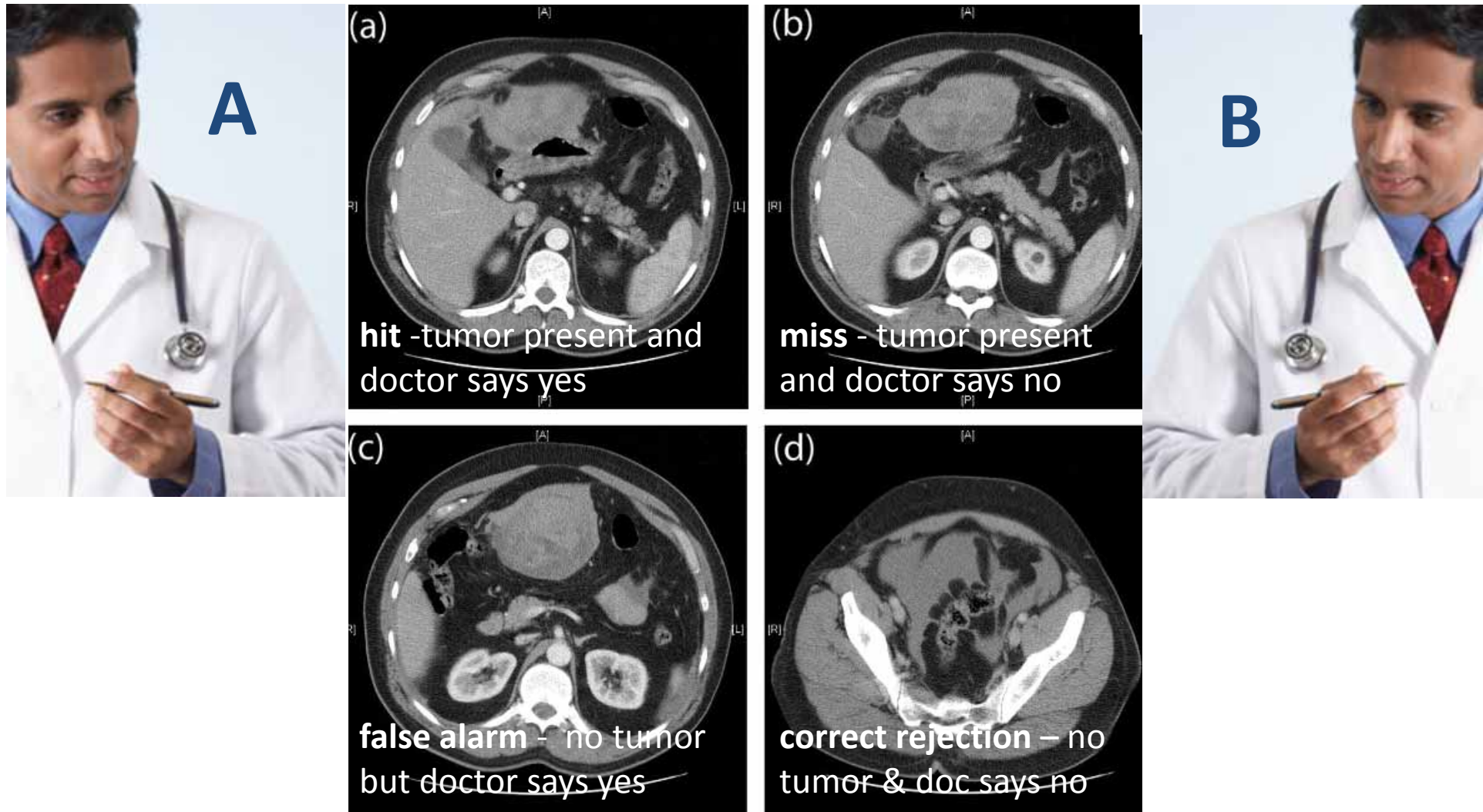
Further, we obtain

$$p(\text{health}(t) = h | \mathbf{X}) = p(h | \mathbf{V}) \prod_{U \in \mathbf{U}} p(\text{health}(t) \neq \text{death} | U, \text{health}(t-1))$$

for $h \neq \text{death}$

van Gerven, M. A. J., Taal, B. G. & Lucas, P. J. F. (2008) Dynamic Bayesian networks as prognostic models for clinical patient management. *Journal of Biomedical Informatics*, 41, 4, 515-529.

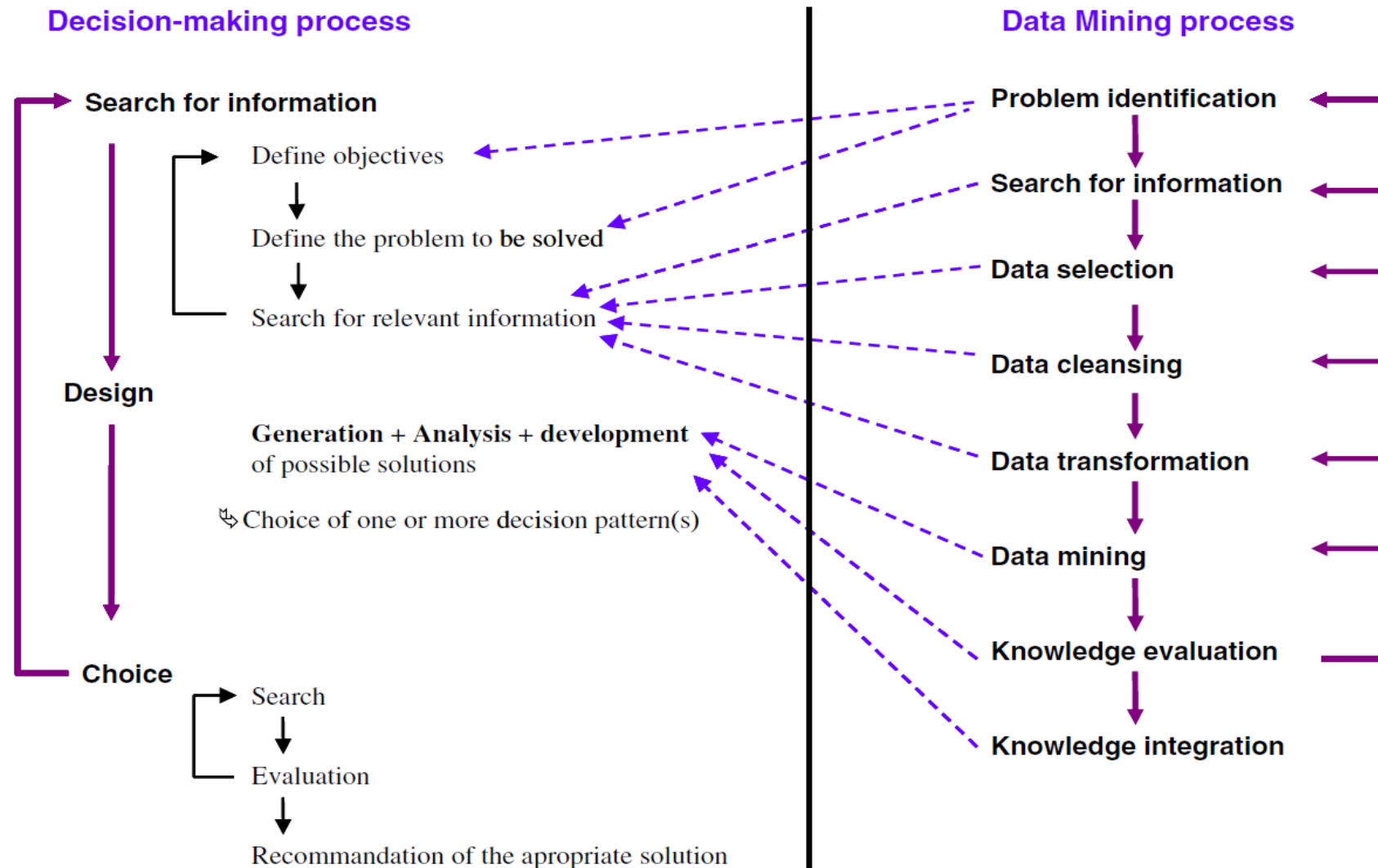
What for?



Two doctors, with equally good training, looking at the same CT scan, will have the same information ... but they may have a different bias/criteria!

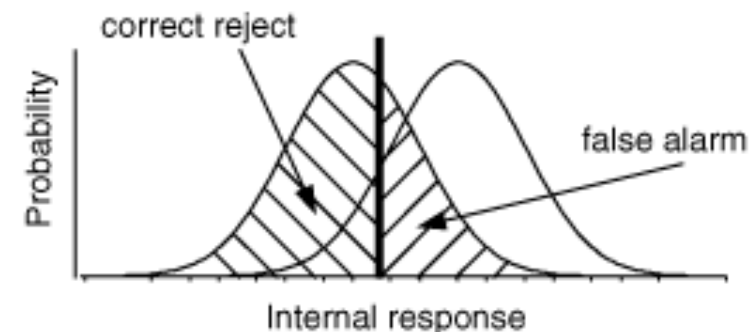
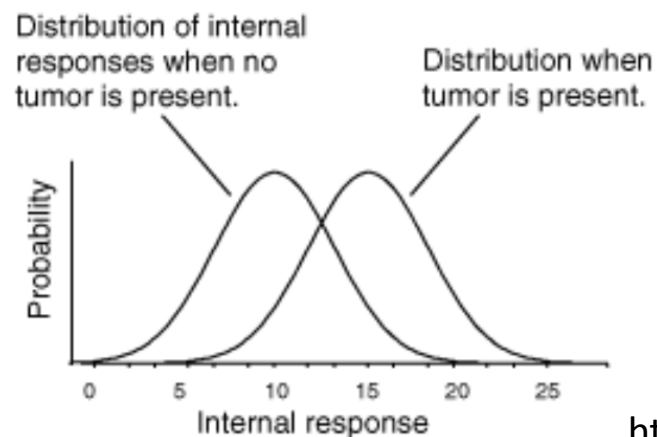
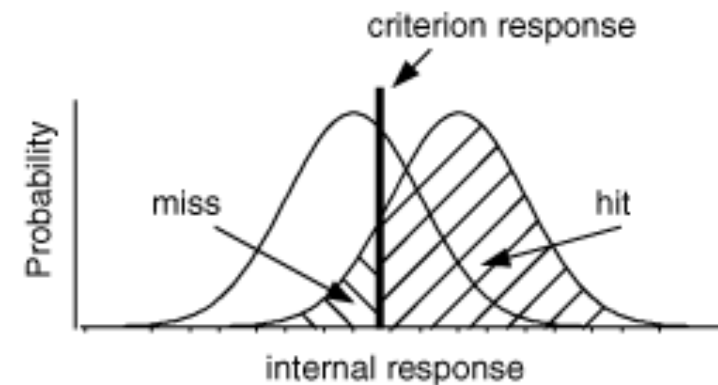
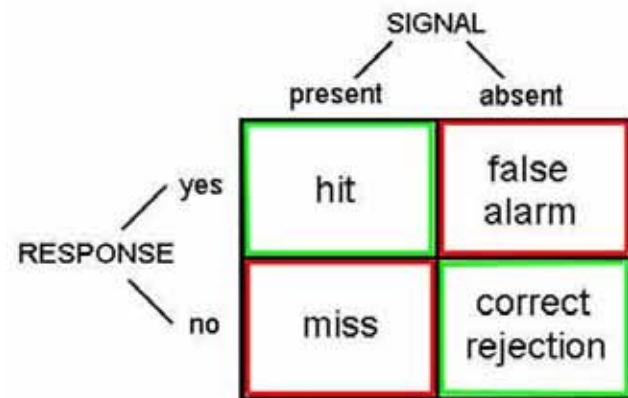
- **Information acquisition:** in the CT data, e.g. healthy lungs have a characteristic shape; the presence of a tumor might distort that shape (= anomaly).
- Tumors have different image characteristics: brighter or darker, different texture, etc.
- With proper training a doctor learns what kinds of things to look for, so with more practice/training they will be able to acquire more (and more reliable) information.
- Running another test (e.g., MRI) can be used to acquire more (relevant!) information.
- The effect of information is to increase the likelihood of getting either a hit or a correct rejection, while reducing the likelihood of an outcome in the two error boxes (slide 33).
- **Criterion:** Additionally to relying on technology/testing, the medical profession allows doctors to use their own judgment.
- Different doctors may feel that the different types of errors are not equal.
- For example, a doctor may feel that missing an opportunity for early diagnosis may mean the difference between life and death.
- A false alarm, on the other hand, may result only in a routine biopsy operation. They may chose to err toward ``yes" (tumor present) decisions.
- Other doctors, however, may feel that unnecessary surgeries (even routine ones) are very bad (expensive, stress, etc.).
- They may chose to be more conservative and say ``no" (no tumor) more often. They will miss more tumors, but they will be doing their part to reduce unnecessary surgeries. And they may feel that a tumor, if there really is one, will be picked up at the next check-up.

Mohamed, A. et al. (2010) Traumatic rupture of a gastrointestinal stromal tumour with intraperitoneal bleeding and haematoma formation. *BMJ Case Reports*, 2010.



Ayed, B. M., Ltifi, H., Kolski, C. & Alimi, A. (2010) A user-centered approach for the design & implementation of KDD-based DSS: A case study in the healthcare domain. *Decision Support Systems*, 50, 64-78.

Remember: Two doctors, with equally good training, looking at the same CT scan data, will have the same information ... but they may gain different knowledge due to *bias/criteria*.

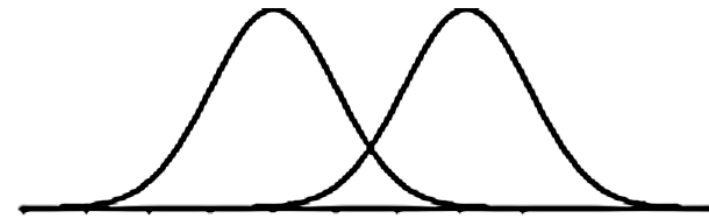


<http://www-psych.stanford.edu/~lera/psych115s/notes/signal>

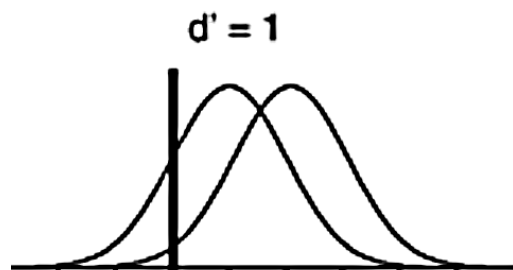
For an example see: Braga & Oliveira (2003) Diagnostic analysis based on ROC curves: theory and applications in medicine. *Int. Journal of Health Care Quality Assurance*, 16, 4, 191-198.



$d' = 1$ (lots of overlap)



$d' = 3$ (not much overlap)

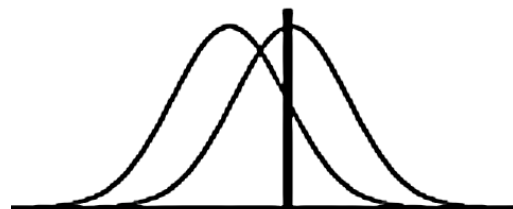


$d' = 1$

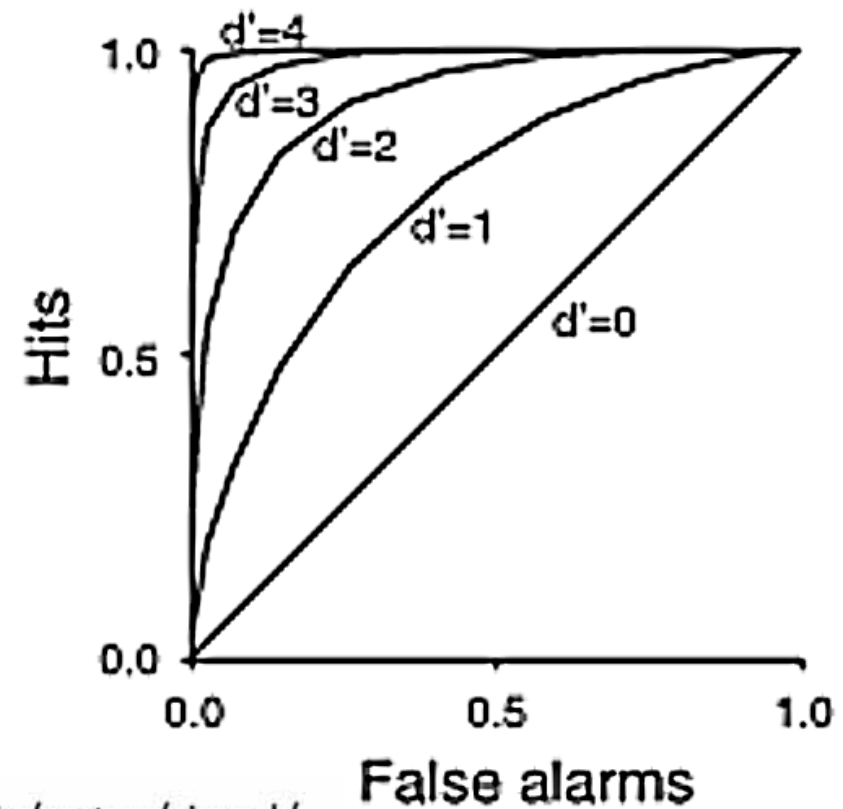
Hits = 97.5%
False alarms = 84%



Hits = 84%
False alarms = 50%



Hits = 50%
False alarms = 16%



<http://www-psych.stanford.edu/~lera/psych115s/notes/signal/>

Probable Information $P(x)$

Sum Rule Σ

$$P(x) = \sum_{x \in X} P(x, y)$$



Thomas Bayes
1701 - 1761

Product Rule \prod

$$P(x, y) = P(y|x)P(x)$$

Bayes' Rule is a corollary of Sum Rule and Product Rule:

$$P(x|y) = \frac{P(y|x)P(x)}{\sum_{x \in X} P(x, y) P(x)}$$

Bayes' Rule in words

d ... data; h ... hypothesis

$$P(h|d) = \frac{P(d|h)P(h)}{P(d)}$$

$P(h)$: prior belief (probability of hypothesis h before seeing any data)

$P(d|h)$: likelihood (probability of the data if the hypothesis h is true)

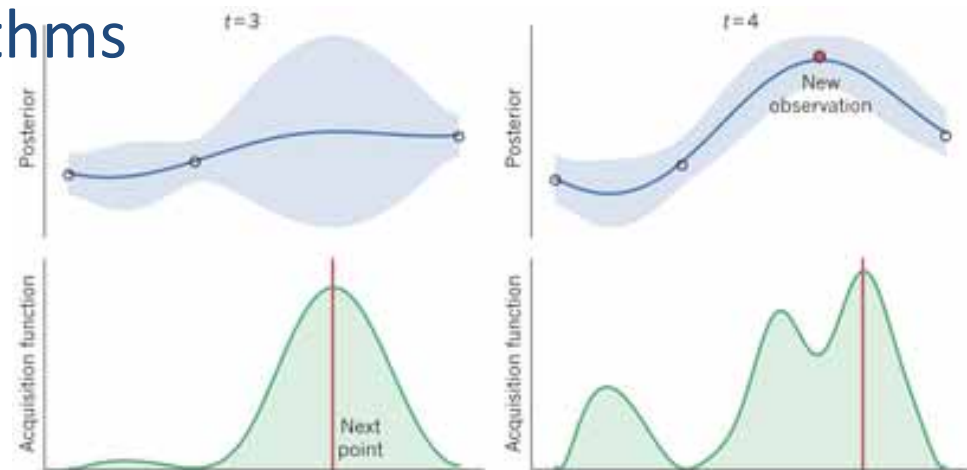
$P(d) = \sum_h P(d|h)P(h)$: data evidence (marginal probability of the data)

$P(h|d)$: posterior (probability of hypothesis h after having seen the data d)

$$\text{posterior} = \frac{\text{likelihood} * \text{prior}}{\text{evidence}}$$

The inverse probability allows to infer unknowns, learn from data and make predictions = machine learning!

- Many aspects of intelligence and learning depend on **probabilistic representation of uncertainty**:
- Forecasting
- Decision support
- Learning from noisy, missing, uncertain data ...
- Knowledge discovery
- Probabilistic programming (e.g. Stochastic Python, Julia)
- Universal inference algorithms
- Global optimization



Ghahramani, Z. 2015. Probabilistic machine learning and artificial intelligence. Nature, 521, (7553), 452-459.

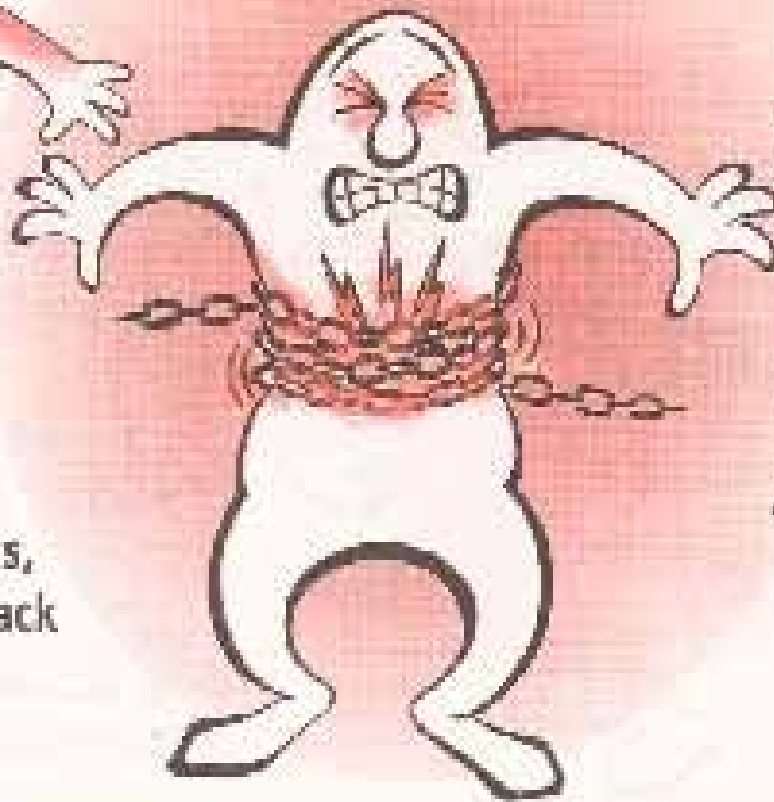
Learn the

Heart attack warning signs!



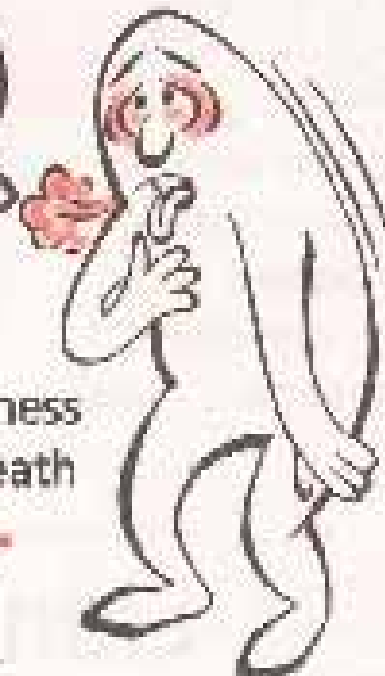
Pain in the
jaw, neck, arms,
shoulders, or back

Chest pressure,
squeezing, or pain



Nausea, sweating,
or feeling faint

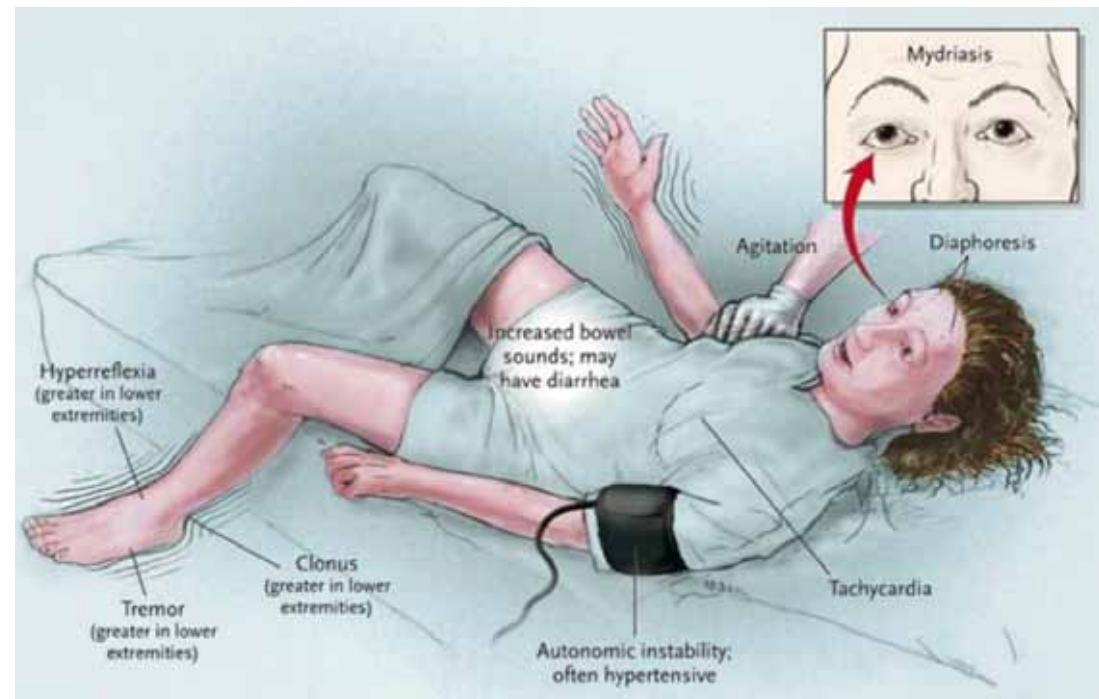
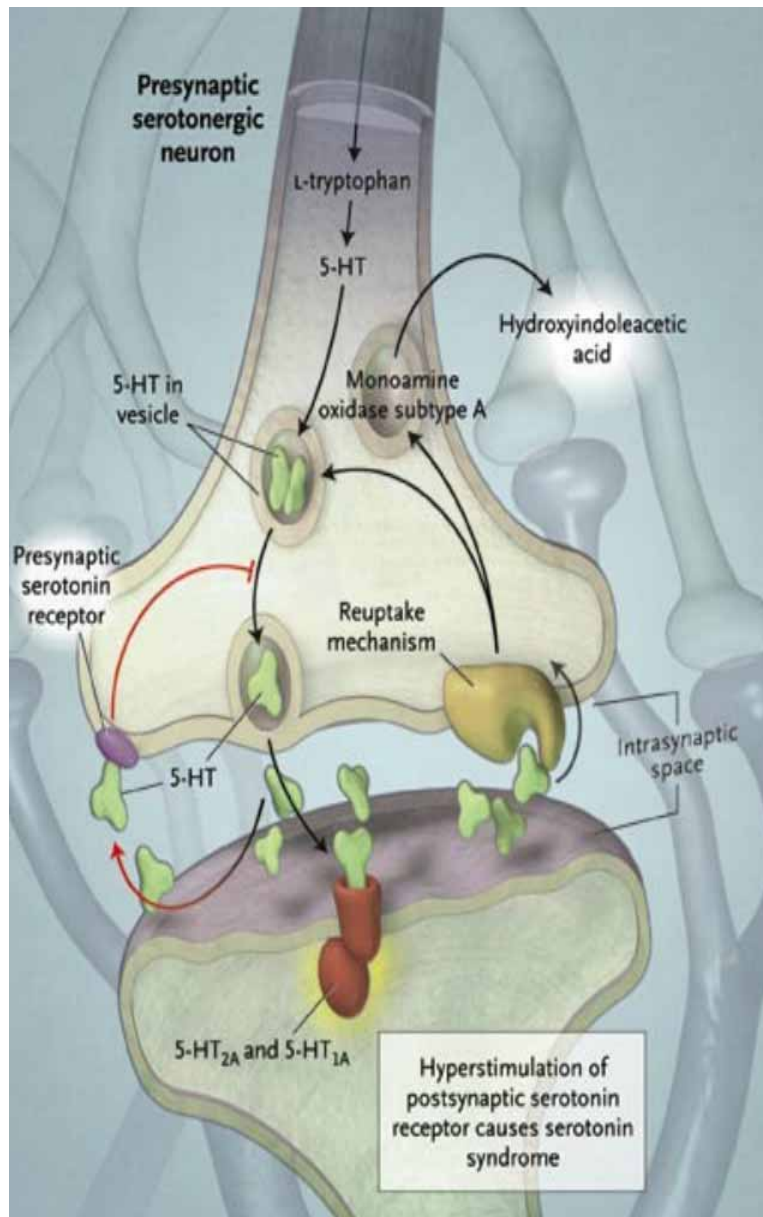
Shortness
of breath



partACT

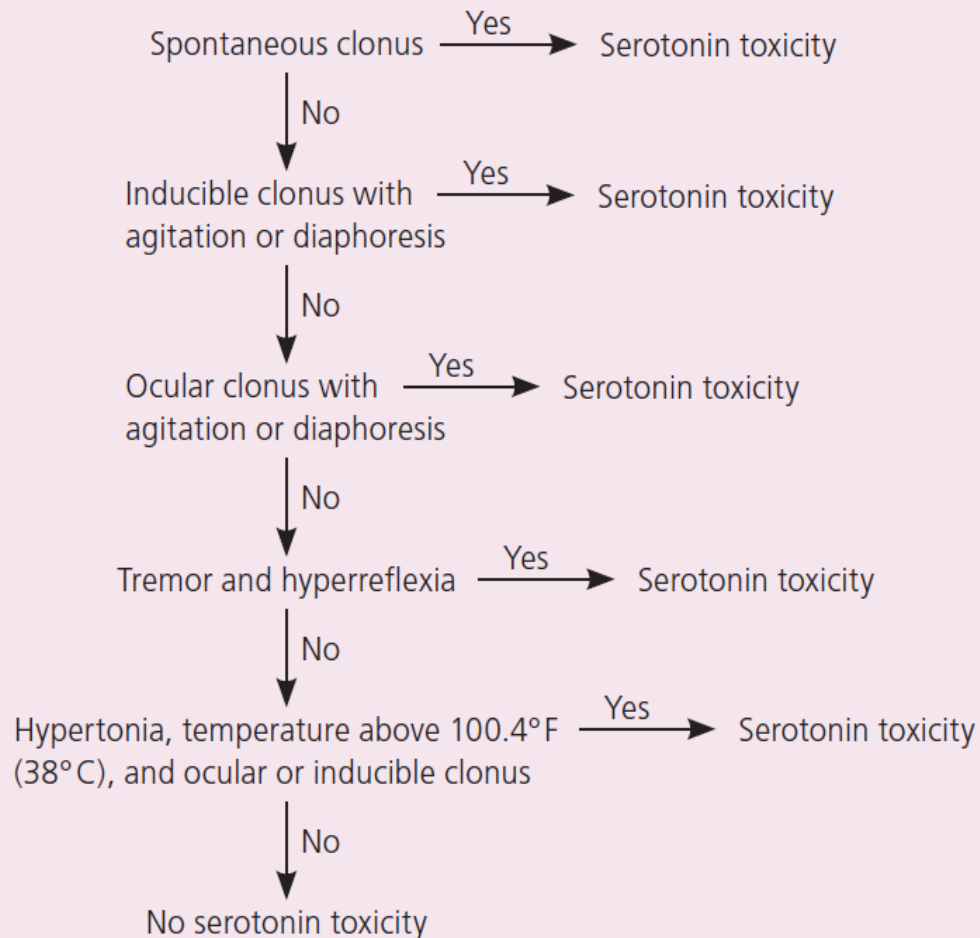
Act Fast! Call 9-1-1

- Clinical Example:
- D ... acute heart attack
- U_+ ... instable chest pain
- $p(D)$... 37 of 1000 = 0,037 (heart attack)
- $p(\bar{D})$... 963 of 1000 = 0,963 (no heart attack)
- 40% of patients report on instable chest pain
- $p(U_+|D) = 0,4$
- Unfortunately this symptoms also occur in 5 % of the healthy population
- $p(U_+|\bar{D}) = 0,05$
- We find the probability for a heart attack during this symptoms therefore by using Bayes' Rule:
- $$p(D|U_+) = \frac{p(U_+|D) * p(D)}{p(U_+|D) * p(D) + p(U_+|\bar{D}) * p(\bar{D})} = 0,235$$



Boyer, E. W. & Shannon, M. (2005) The Serotonin Syndrome. *New England Journal of Medicine*, 352, 11, 1112-1120.

Hunter's Decision Rules for Diagnosis of Serotonin Toxicity

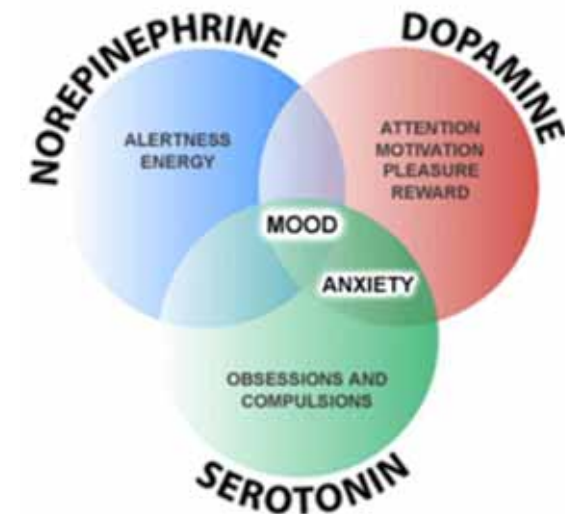


Signs & Symptoms of Serotonin Syndrome

Agitation (restlessness)*	Multi-organ failure†
Diaphoresis*	Myoclonus*
Diarrhea*	Ocular clonus
Disseminated intravascular coagulation†	Rhabdomyolysis†
Fever above 100.4°F (38°C)	Shivering*
Hyperreflexia*	Tonic-clonic seizures†
Incoordination (ataxia)*	Tremor*
Mental status changes	
Confusion*	
Hypomania*	

*—Sternbach's diagnostic criteria require three of 10 signs and symptoms.
 †—Extremely severe cases.

Ables, A. Z. & Nagubilli, R. (2010) Prevention, recognition, and management of serotonin syndrome. *American family physician*, 81, 9, 1139.

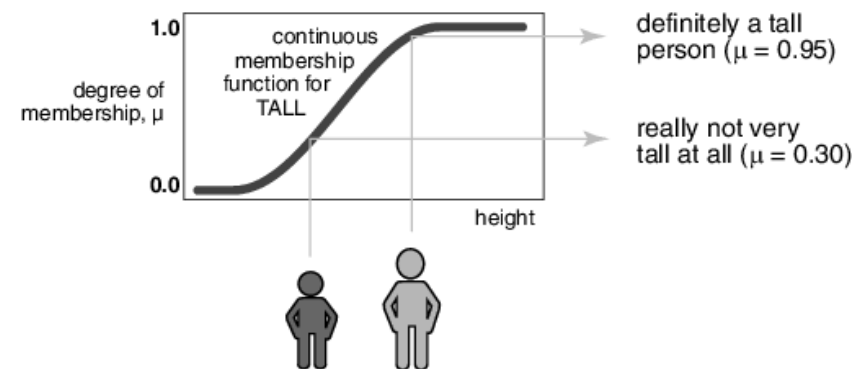
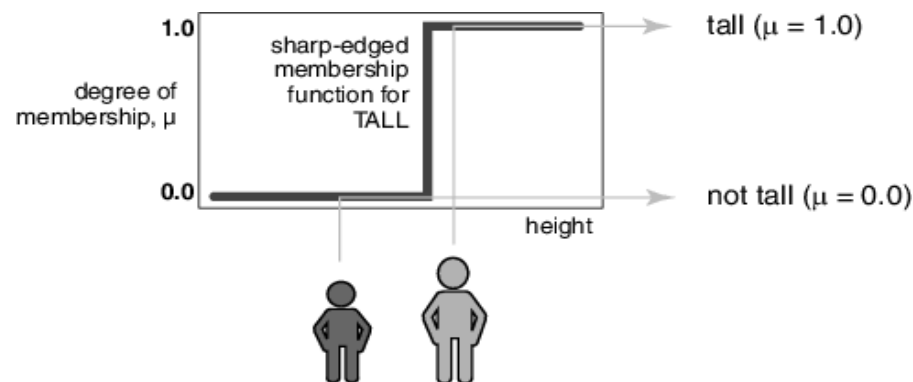


<i>Clinical condition</i>	<i>History</i>	<i>Vital signs</i>	<i>Clinical features</i>
Anticholinergic syndrome	Use of tricyclic antidepressants or other anticholinergic drugs	Tachycardia, tachypnea, hyperthermia (usually 102.2° F [39° C] or below)	Dry mouth, blurred vision, mydriasis, flushed skin, agitation/delirium, decreased bowel sounds
Malignant hyperthermia	Administration of halogenated inhalational anesthetics or depolarizing muscle relaxants	Hypertension, tachycardia, tachypnea, hyperthermia (up to 114.8° F [46° C])	Diaphoresis, mottled skin, agitation, decreased bowel sounds, muscular rigidity, hyporeflexia
Neuroleptic malignant syndrome	Ingestion of antipsychotic medications	Hypertension, tachycardia, tachypnea, hyperthermia (above 105.8° F [41° C])	Sialorrhea, diaphoresis, pallor, stupor, mutism, coma, normal or decreased bowel sounds, lead-pipe rigidity, bradyreflexia

Ables, A. Z. & Nagubilli, R. (2010) Prevention, recognition, and management of serotonin syndrome. *American family physician*, 81, 9, 1139.

**What can we do if we
have not only
probabilistic, but also
incomplete data ...**

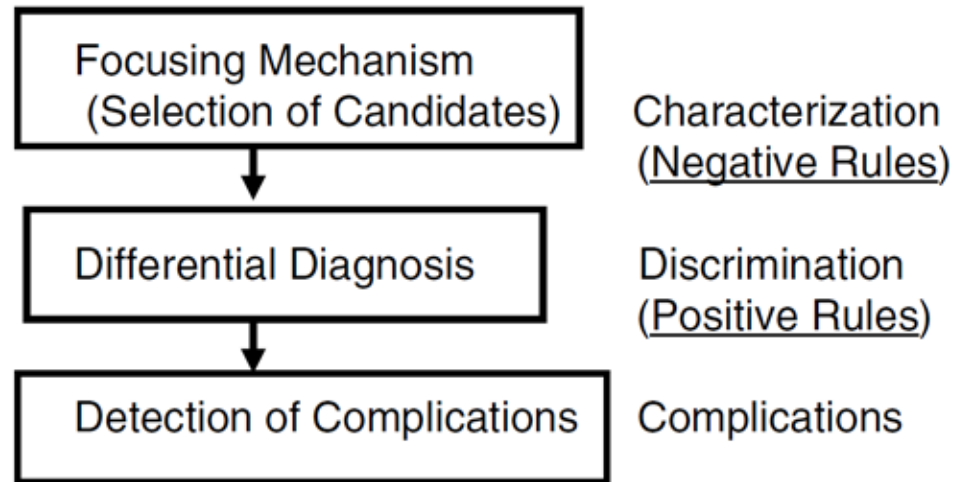
Rough Set Theory



<https://www.calvin.edu/~pribeiro/othrlnks/Fuzzy/fuzzyeng.htm>

- ... is an extension of the Classical Set Theory, for use when representing incomplete knowledge.
- RS are sets *with fuzzy boundaries* – sets that cannot be precisely characterized using the available set of attributes, exactly like it is in medical decision making; based on 2 ideas:
- 1) a given concept can be approximated by partition-based knowledge as upper and lower approximation – which corresponds to the focusing mechanism of differential medical diagnosis: upper approximation as selection of candidates and lower approximation as concluding a final diagnosis.
- 2) a concept or observation can be represented as partitions in a given data set, where rough sets provides a rule induction method from given data. Thus, this model can be used to extract rule-based knowledge from medical databases.

Example Symptom: Headache



Tsumoto, S. (2006) Pawlak Rough Set Model, Medical Reasoning and Rule Mining. In: Greco, S., Hata, Y., Hirano, S., Inuiguchi, M., Miyamoto, S., Nguyen, H. & Slowinski, R. (Eds.) *Rough Sets and Current Trends in Computing*. Berlin, Heidelberg, Springer, 53-70.

Let U denote a non-empty, finite set called the universe
and A denote a non-empty, finite set of attributes:

- $a : U \rightarrow V_a$ for $a \in A$
- where V_a is called the domain of a
- Then, the decision table is defined as an information system:
- $A = (U, A \cup \{d\})$.
- The table shows an example of an information system with
- $U = \{1, 2, 3, 4, 5, 6\}$ and
- $A = \{\text{age, location, nature, prodrome, nausea, M1}\}$ and
- $d = \text{class}$.
- For $\text{location} \in A$, V_{location} is defined as $\{\text{occular, lateral, whole}\}$

No.	age	location	nature	prodrome	nausea	M1	class
1	50-59	occular	persistent	no	no	yes	m.c.h.
2	40-49	whole	persistent	no	no	yes	m.c.h.
3	40-49	lateral	throbbing	no	yes	no	migra
4	40-49	whole	throbbing	yes	yes	no	migra
5	40-49	whole	radiating	no	no	yes	m.c.h.
6	50-59	whole	persistent	no	yes	yes	psycho

DEFINITIONS. M1: tenderness of M1, m.c.h.: muscle contraction headache, migra: migraine, psycho: psychological pain.

Tsumoto, S. (2006) Pawlak Rough Set Model, Medical Reasoning and Rule Mining. In: Greco, S., Hata, Y., Hirano, S., Inuiguchi, M., Miyamoto, S., Nguyen, H. & Slowinski, R. (Eds.) *Rough Sets and Current Trends in Computing*. Berlin, Heidelberg, Springer, 53-70.

Is there another possibility?

- 1) Logic
- 2) Statistics/Probability
- 3) Heuristics

Judgment under Uncertainty: Heuristics and Biases

Biases in judgments reveal some heuristics of
thinking under uncertainty.

Amos Tversky and Daniel Kahneman

Many decisions are based on beliefs concerning the likelihood of uncertain events such as the outcome of an election, the guilt of a defendant, or the future value of the dollar. These beliefs are usually expressed in statements such as "I think that . . . ," "chances are . . . ," "it is unlikely that . . . ," and so forth. Occasionally, beliefs concerning uncertain events are expressed in numerical form as odds or subjective probabilities. What determines such beliefs? How do people assess the prob-

ability of uncertain events? Judgments are often made when visibility is good because the objects are seen sharply. Thus, the reliance on clarity as an indication of distance leads to common biases. Such biases are also found in the intuitive judgment of probability. This article describes three heuristics that are employed to assess probabilities and to predict values. Biases to which these heuristics lead are enumerated, and the applied and theoretical implications of these observations are discussed.

occupation from a list of possibilities (for example, farmer, salesman, airline pilot, librarian, or physician)? How do people order these occupations from most to least likely? In the representativeness heuristic, the probability that Steve is a librarian, for example, is assessed by the degree to which he is representative of, or similar to, the stereotype of a librarian. Indeed, research with problems of this type has shown that people order the occupations by probability and by similarity in exactly the same way (1). This approach to the judgment of probability leads to serious errors, because similarity, or representativeness, is not influenced by several factors that should affect judgments of probability.

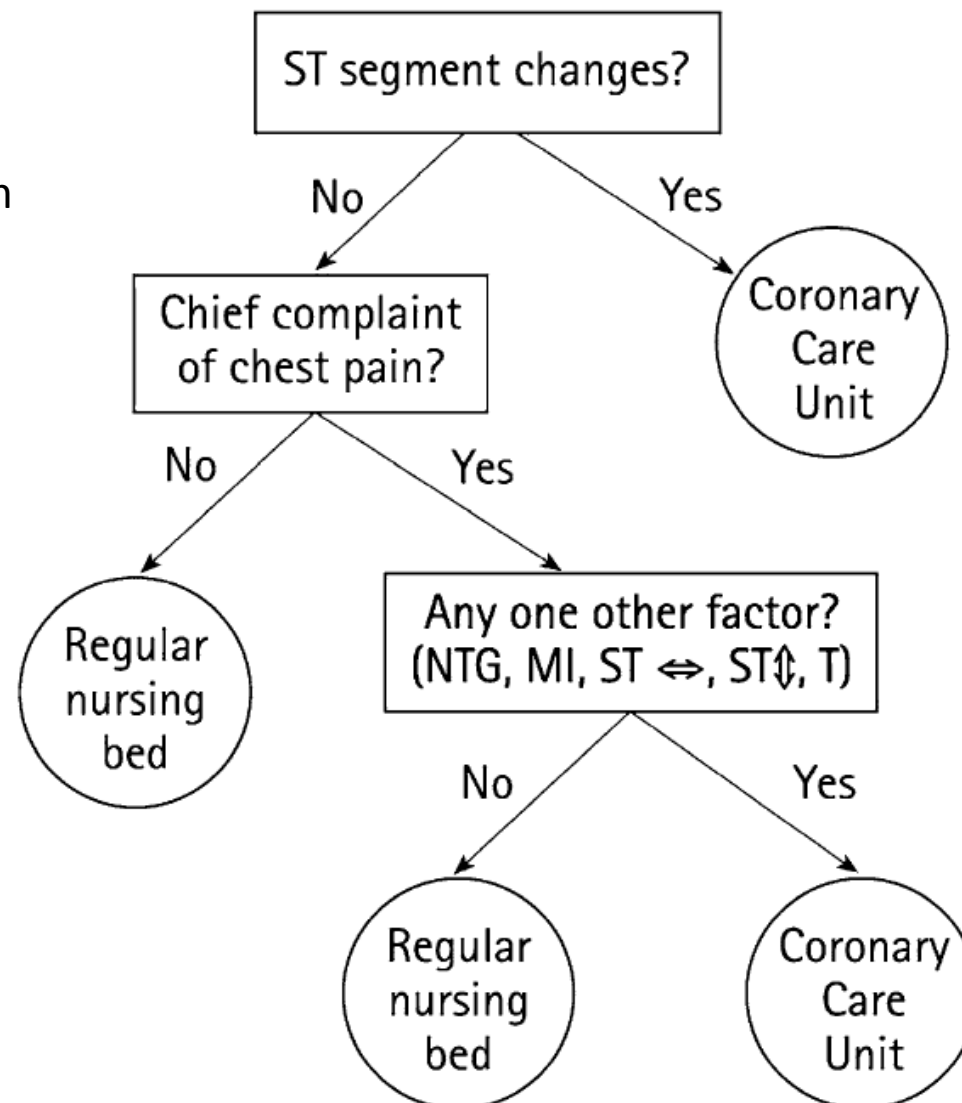
Insensitivity to prior probability of outcomes. One of the factors that have no effect on representativeness but should have a major effect on probability is the prior probability, or base-rate frequency, of the outcomes. In the case of Steve, for example, the fact that there are many more farmers than librarians in the population should enter into any reasonable estimate of the probability that Steve is a librarian rather than a farmer. Considerations of base-rate frequency, however, do not

MI = myocardial infarction

N.A. = not applicable

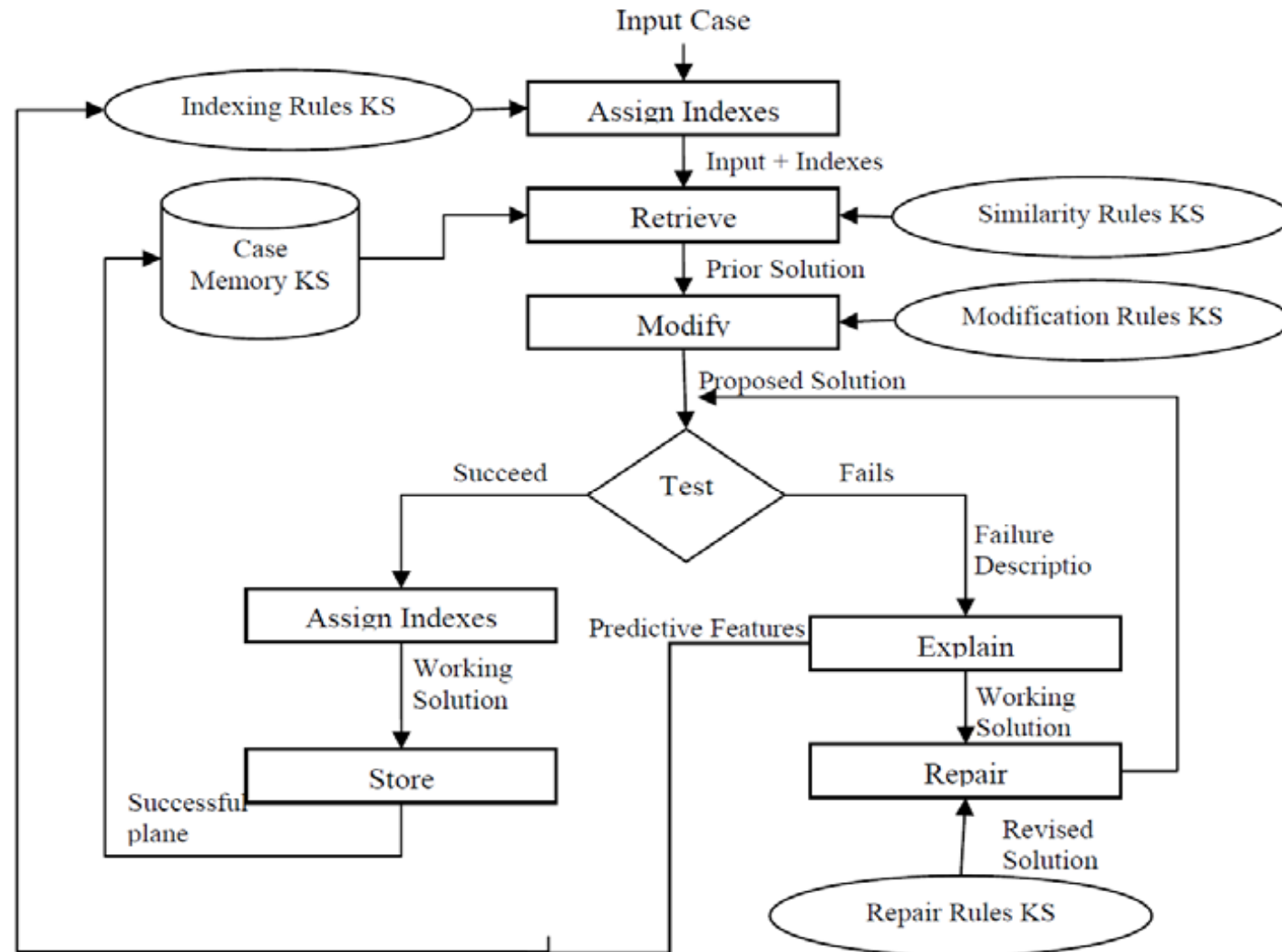
NTG = nitroglycerin

T= T-waves with peaking or inversion



Gigerenzer, G. & Gaissmaier, W. (2011) Heuristic Decision Making. In: Fiske, S. T., Schacter, D. L. & Taylor, S. E. (Eds.) *Annual Review of Psychology*, Vol 62. Palo Alto, *Annual Reviews*, 451-482.

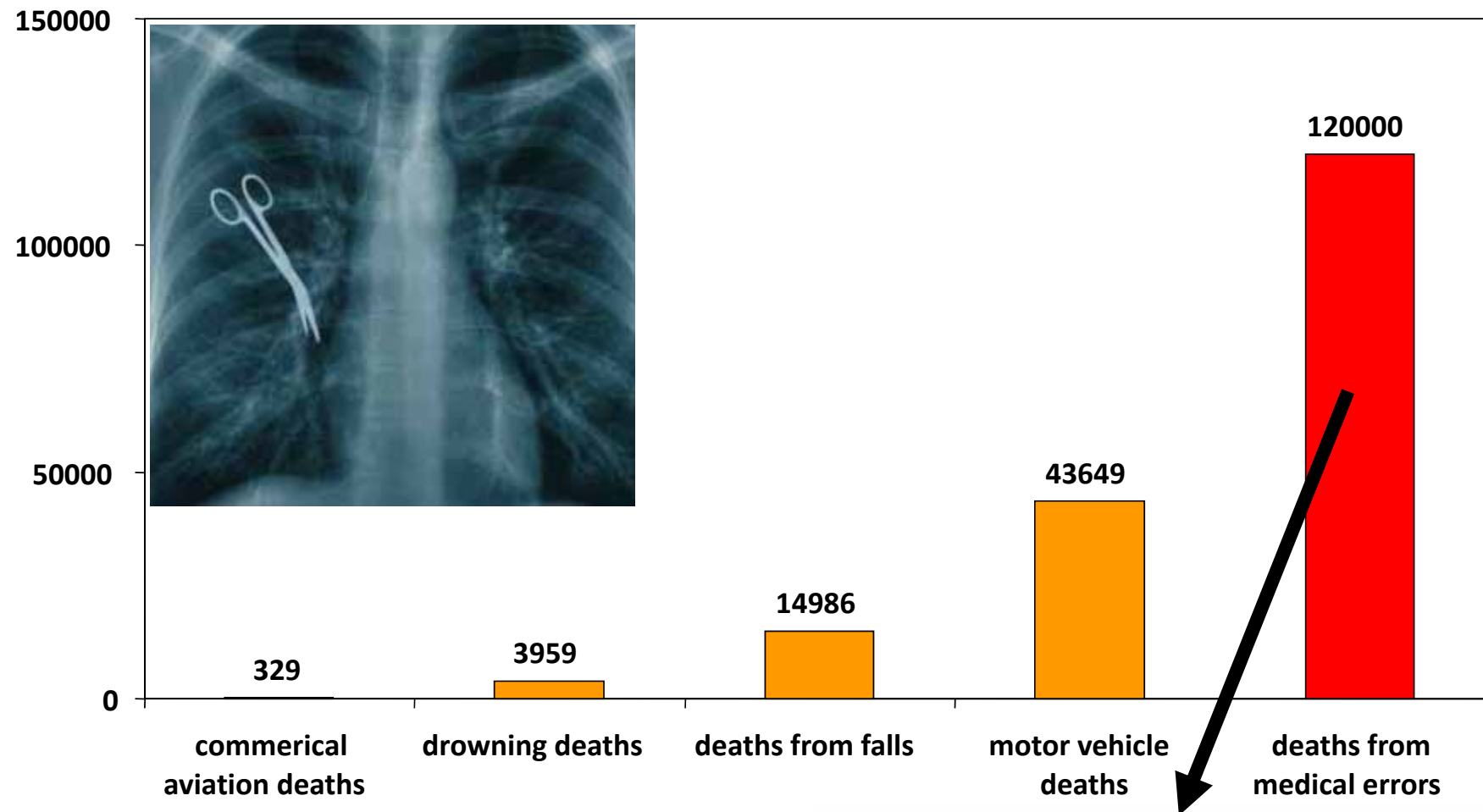
Boxes =
processes;
ovals =
knowledge
structures (KS)



Salem, A. B. M. (2007) Case based reasoning technology for medical diagnosis.
Proc. World Academy of Science, Engineering and Technology, 25, 9-13.

Human Error





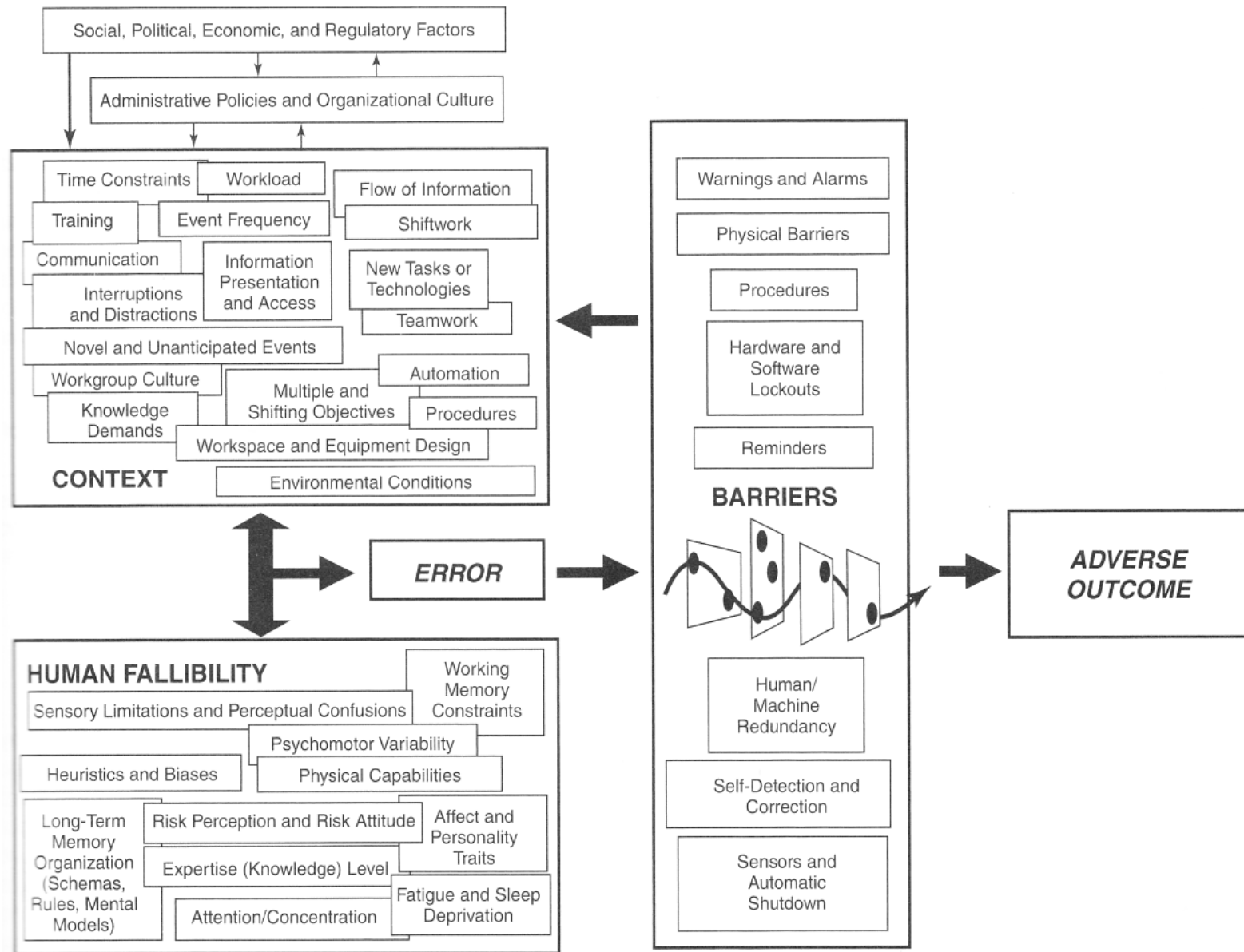
One jumbo jet crash every day



Kohn, L. T., Corrigan, J. M. & Donaldson, M. S. (1999) *To Err Is Human: Building a Safer Health System*; Washington (DC), The Institute of Medicine (IOM).

- Medical error = any failure of a planned action;
- Serious ME = causes harm; includes preventable adverse events, intercepted serious errors, and non-intercepted serious errors. Does not include trivial errors with little or no potential for harm or non-preventable adverse events;
- Intercepted serious error = is caught before reaching patients;
- Non-intercepted serious error = reaches the patient but of good fortune or sufficient reserves to buffer the error, it did not cause harm;
- Adverse event = any injury (e.g. a rash caused by an antibiotic, deep vein thrombosis following omission to continue prophylactic subcutaneous heparin orders on transfer to the critical care unit, ventricular tachycardia due to placement of a central venous catheter tip in the right ventricle etc.);
- Non-preventable adverse event = Unavoidable injury due to appropriate medical care.
- Preventable adverse event = Injury due to a non- intercepted serious error in medical care.

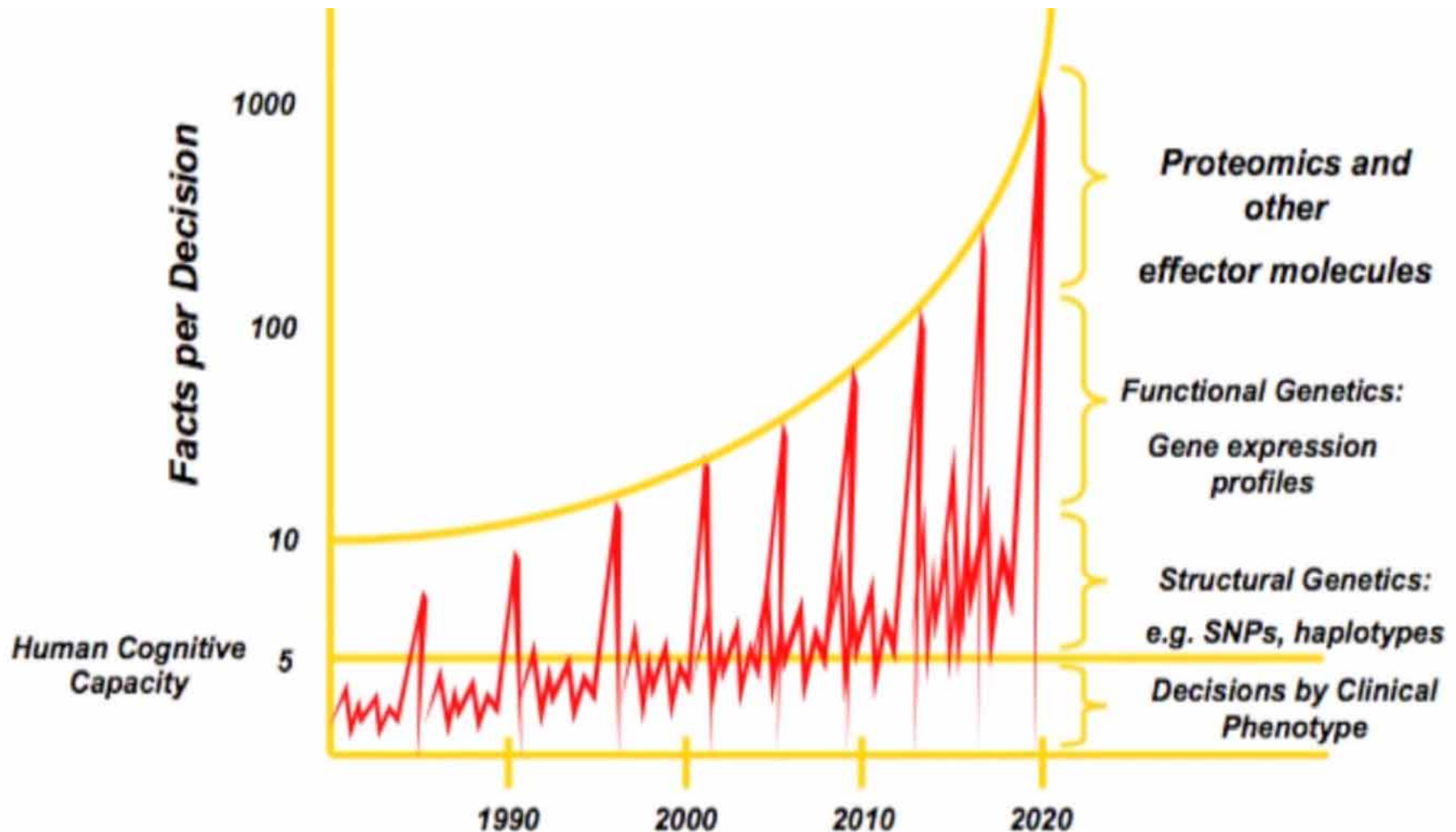
Rothschild et al. (2005) The Critical Care Safety Study: The incidence and nature of adverse events and serious medical errors in intensive care. *Critical Care Medicine*, 33, 8, 1694.



Sharit, J. (2006)
Human Error. In:
Salvendy, G.
(Ed.) *Handbook
of Human
Factors and
Ergonomics,
Third Edition.*
Hoboken (NJ),
Wiley, 708-760.



Thank you!



William Stead, IOM Meeting, 8 October 2007. Growth in facts affecting provider decisions versus human cognitive capacity.

- What is still considered the main and central topic in medical informatics?
- Please explain the information flow within the memory system according to Atkinson & Shiffrin!
- Explain the general model of human information processing following the model of Wickens!
- Explain the processing of visual (image, pictorial) information!
- What is so different in the alternative memory model according to Baddeley (1986)?
- Why is Attention of importance for medical informatics?
- Please explain the process of human decision making according to the model of Wickens (1984)!
- What is Triage?
- Please explain the hypothesis-oriented algorithm for Clinicians!
- What is the big difference between the Hypothetico-Deductive Method and the Plan-Do-Check-Act Deming Model?
- How can we model patient health – please provide an example!

- Please contrast the decision making process with the data mining process!
- Why is Signal Detection Theory important for us?
- Please provide an Example for the application of Bayes' Theorem!
- How does Differential Diagnosis work?
- How can we apply Rough Set Theory for differential diagnostics?
- What is Heuristic Decision Making?
- What is problematic when dealing with heuristic decision making from an informatics viewpoint?
- What is Case Based Reasoning (CBR)?
- How are medical errors defined?
- How does the framework for understanding human error work?

- <http://www.anaesthetist.com/mnm/stats/roc>
- <http://sbml.org>
- <http://www.hci4all.at>
- <http://www.lcb.uu.se/tools/rosetta>
- <http://wise.cgu.edu/sdtmod/overview.asp>
(excellent Tutorial on SDT)
- <http://www.iom.edu> (Institute of Medicine)
- <http://www.ahrq.gov/qual/patientsafetyix.htm>
(Agency for Health Care Research and Quality)
- <http://www.fda.gov/drugs/drugsafety/medicationerrors/default.htm> (Food and Drug Administration, FDA, medication errors)

Hunt, S.,
Miller, A. L.,
Schissel, S. &
Ross, J. J.
(2010) A
Crazy Cause
of Dyspnea.
Interactive
Multimedia
Case New
England
Journal of
Medicine,
363, 25, e38.

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INTERACTIVE MEDICAL CASE
Graham T. McMahon, M.D., M.M.Sc., Editor, Joel T. Katz, M.D., Associate Editor, Bruce D. Levy, M.D., Associate Editor, Joseph Loscalzo, M.D., Ph.D., Associate Editor

A Crazy Cause of Dyspnea

Susan Hunt, M.D., Amy Leigh Miller, M.D., Scott Schissel, M.D., and John J. Ross, M.D.
N Engl J Med 2010; 363:e38 | [December 16, 2010](#)

Case

An 18-year-old black woman presented with fever, ear pain, and dull discomfort on the right side of the chest that was unchanged with movement or inspiration. She had no other symptoms and had previously been well, aside from mild exercise-induced asthma. Chest radiography was performed, and the images showed air-space opacities in the base of the right lung and the perihilar region of the left lung.



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[Medical Practice, Training, and Education](#) [Pulmonary/Critical Care General](#)

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[Clinical Cases](#) [December 16, 2010](#)

TRENDS: MOST VIEWED (Last Week)

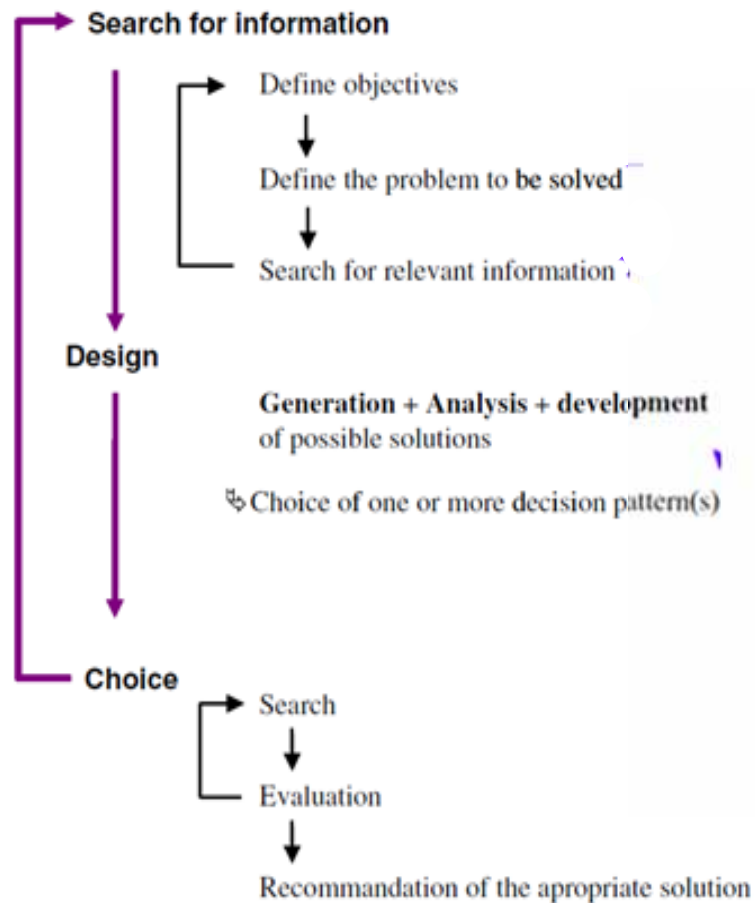
- [Rivaroxaban in Patients with a Recent Acute Coronary Syndrome](#)
- [Intensive Diabetes Therapy and Glomerular Filtration Rate in Type 1 Diabetes](#)
- [Dronedarone in High-Risk Permanent Atrial Fibrillation](#)

[More Trends](#)

<http://www.nejm.org/doi/full/10.1056/NEJMimc1008281>

- 1. Intro: Computer Science meets Life Sciences, challenges, future directions
- 2. Back to the future: Fundamentals of Data, Information and Knowledge
- **3. Structured Data: Coding, Classification (ICD, SNOMED, MeSH, UMLS)**
- 4. Biomedical Databases: Acquisition, Storage, Information Retrieval and Use
- 5. Semi structured and weakly structured data (structural homologues)
- 6. Multimedia Data Mining and Knowledge Discovery
- 7. Knowledge and Decision: Cognitive Science & Human-Computer Interaction
- 8. Biomedical Decision Making: Reasoning and Decision Support
- 9. Intelligent Information Visualization and Visual Analytics
- 10. Biomedical Information Systems and Medical Knowledge Management
- 11. Biomedical Data: Privacy, Safety and Security
- 12. Methodology for Info Systems: System Design, Usability & Evaluation

Decision-making process



Data Mining process



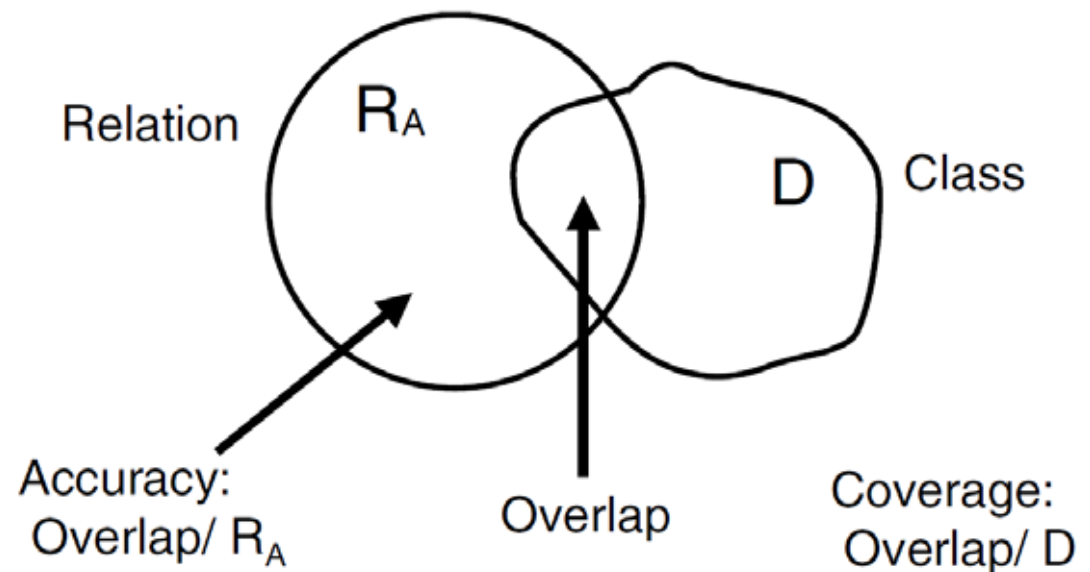
- The atomic formula over
- $B \subseteq A \cup \{d\}$ and V are expressions of the form $[a = v]$
- called descriptors over B , where $a \in B$ and $v \in V_a$.
- The set $F(B, V)$ of formulas over B is the least set containing all atomic formulas over B and closed with respect to disjunction, conjunction and negation. For example, $[\text{location} = \text{ocular}]$ is a descriptor of B .
- For each $f \in F(B, V)$, f_A denote the meaning of f in A , i.e., the set of all objects in U with property f , defined inductively as follows.
 - 1. If f is of the form $[a = v]$ then, $f_A = \{s \in U \mid a(s) = v\}$
 - 2. $(f \wedge g)_A = f_A \cap g_A$; $(f \vee g)_A = f_A \cup g_A$; $(\neg f)_A = U - f_A$
- For example, $f = [\text{location} = \text{whole}]$ and $f_A = \{2, 4, 5, 6\}$. As an example of a conjunctive formula, $g = [\text{location} = \text{whole}] \wedge [\text{nausea} = \text{no}]$ is a descriptor of U and f_A is equal to $g_{\text{location, nausea}} = \{2, 5\}$.

Definition 1. Let R and D denote a formula in $F(B, V)$ and a set of objects which belong to a decision d . Classification accuracy and coverage (true positive rate) for $R \rightarrow d$ is defined as:

$$\alpha_R(D) = \frac{|R_A \cap D|}{|R_A|} (= P(D|R)), \text{ and}$$

$$\kappa_R(D) = \frac{|R_A \cap D|}{|D|} (= P(R|D)),$$

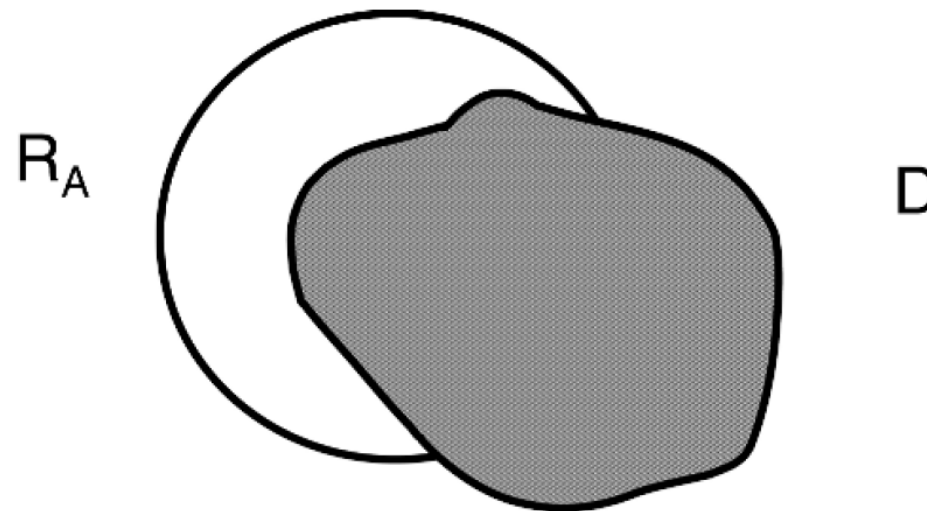
where $|S|$, $\alpha_R(D)$, $\kappa_R(D)$ and $P(S)$ denote the cardinality of a set S , a classification accuracy of R as to classification of D and coverage (a true positive rate of R to D), and probability of S , respectively.



Tsumoto (2006)

By the use of accuracy and coverage, a probabilistic rule is defined as:

$$R \xrightarrow{\alpha, \kappa} d \quad s.t. \quad R = \bigwedge_j [a_j = v_k], \alpha_R(D) \geq \delta_\alpha \\ \text{and } \kappa_R(D) \geq \delta_\kappa,$$



$$R \rightarrow D \quad s.t. \quad \alpha_R(D) > \delta_\alpha, \kappa_R(D) > \delta_\kappa$$

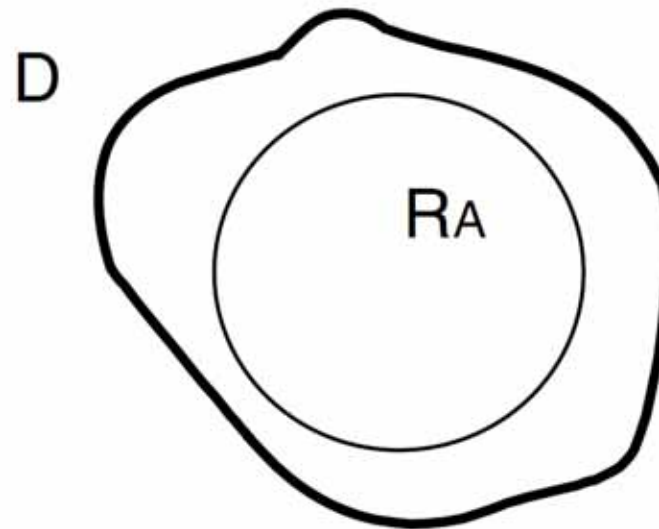
Tsumoto (2006)

A positive rule is defined as a rule supported by only positive examples, the classification accuracy of which is equal to 1.0. It is notable that the set supporting this rule corresponds to a subset of the lower approximation of a target concept, which is introduced in rough sets [1]. Thus, a positive rule is represented as:

$$R \rightarrow d \quad s.t. \quad R = \bigwedge_j [a_j = v_k], \quad \alpha_R(D) = 1.0$$

Figure 4 shows the Venn diagram of a positive rule. As shown in this figure, the meaning of R is a subset of that of D . This diagram is exactly equivalent to the classic proposition $R \rightarrow d$. In the above example, one positive rule of “m.c.h.” (muscle contraction headache) is:

$$[nausea = no] \rightarrow m.c.h. \quad \alpha = 3/3 = 1.0.$$



Tsumoto (2006)

Before defining a negative rule, let us first introduce an exclusive rule, the contrapositive of a negative rule [7]. An exclusive rule is defined as a rule supported by all the positive examples, the coverage of which is equal to 1.0. That is, an exclusive rule represents the necessity condition of a decision. It is notable that the set supporting an exclusive rule corresponds to the upper approximation of a target concept, which is introduced in rough sets [1]. Thus, an exclusive rule is represented as:

$$R \rightarrow d \quad s.t. \quad R = \bigvee_j [a_j = v_k], \quad \kappa_R(D) = 1.0.$$

Figure 4 shows the Venn diagram of a exclusive rule. As shown in this figure, the meaning of R is a superset of that of D . This diagram is exactly equivalent to the classic proposition $d \rightarrow R$. In the above example, the exclusive rule of “m.c.h.” is:

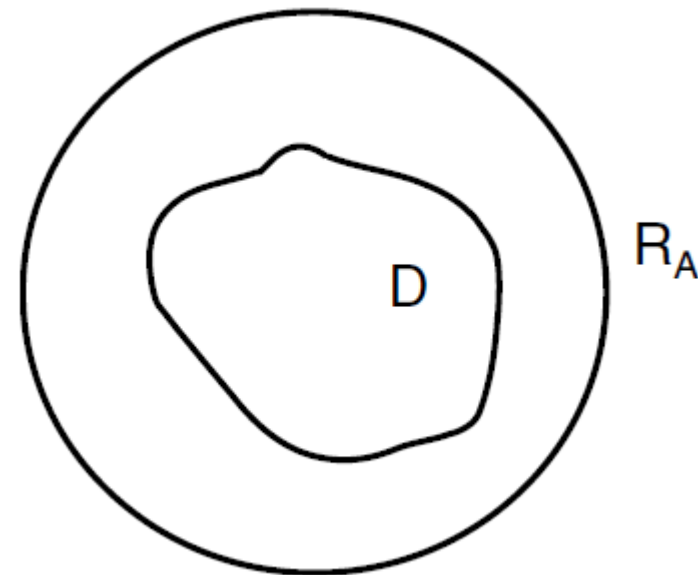
$$[M1 = yes] \vee [nau = no] \rightarrow m.c.h$$

From the viewpoint of propositional logic, an exclusive rule can be represented as:

$$d \rightarrow \bigvee_j [a_j = v_k],$$

because the condition of an exclusive rule corresponds to the upper approximation of conclusion d . Thus, it is easy to see that the contrapositive of an exclusive rule:

$$\bigwedge_j \neg[a_j = v_k] \rightarrow \neg d,$$



Tsumoto (2006)

of conclusion d . Thus, it is easy to see that a negative rule is defined as the contrapositive of an exclusive rule:

$$\bigwedge_j \neg[a_j = v_k] \rightarrow \neg d,$$

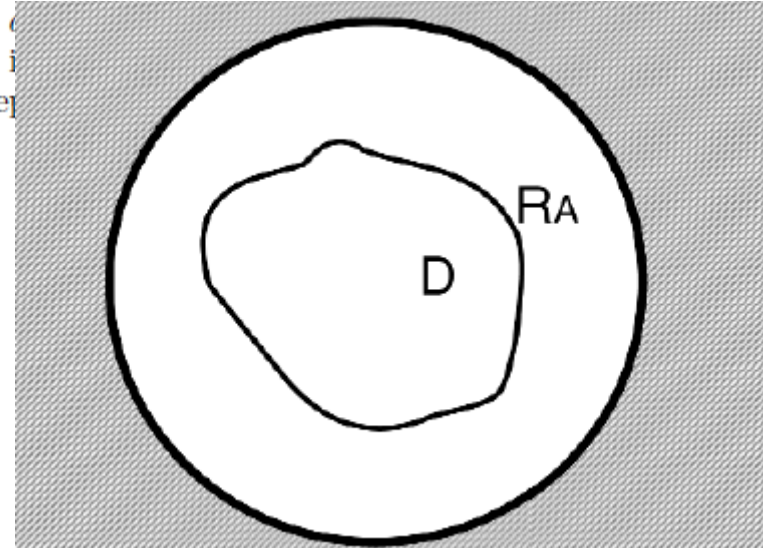
which means that if a case does not satisfy any attribute value pairs in the condition of a negative rule, then we can exclude a decision d from candidates. For example, the negative rule of m.c.h. is:

$$\neg[M1 = yes] \wedge \neg[nausea = no] \rightarrow \neg m.c.h.$$

In summary, a negative rule is defined as:

$$\bigwedge_j \neg[a_j = v_k] \rightarrow \neg d \quad s.t. \quad \forall[a_j = v_k] \kappa_{[a_j=v_k]}(D) = 1.0,$$

where D denotes a set of samples which belong to a class d . Venn diagram of a negative rule. As shown in this figure, the negative region is the “positive region” of “negative concept”



Tsumoto (2006)

```
procedure Exclusive and Negative Rules;  
  var  
     $L$  : List;  
    /* A list of elementary attribute-value pairs */  
  begin  
     $L := P_0$ ;  
    /*  $P_0$ : A list of elementary attribute-value pairs given in a database */  
    while ( $L \neq \{\}$ ) do  
      begin  
        Select one pair  $[a_i = v_j]$  from  $L$ ;  
        if ( $[a_i = v_j]_A \cap D \neq \phi$ ) then do /*  $D$ : positive examples of a target class  $d$  */  
          begin  
             $L_{ir} := L_{ir} + [a_i = v_j]$ ; /* Candidates for Positive Rules */  
            if ( $\kappa_{[a_i = v_j]}(D) = 1.0$ )  
              then  $R_{er} := R_{er} \wedge [a_i = v_j]$ ;  
              /* Include  $[a_i = v_j]$  into the formula of Exclusive Rule */  
            end  
             $L := L - [a_i = v_j]$ ;  
          end  
        Construct Negative Rules:  
        Take the contrapositive of  $R_{er}$ .  
      end {Exclusive and Negative Rules};  
    end
```

The Naïve Bayes Classifier

- What can we do if our data d has several attributes?
- Naïve Bayes assumption: Attributes that describe data instances are conditionally independent given the classification hypothesis

$$P(\mathbf{d} | h) = P(a_1, \dots, a_T | h) = \prod_t P(a_t | h)$$

- it is a simplifying assumption, obviously it may be violated in reality
 - in spite of that, it works well in practice
- The Bayesian classifier that uses the Naïve Bayes assumption and computes the MAP hypothesis is called Naïve Bayes classifier
- One of the most practical learning methods
- Successful applications:
 - Medical Diagnosis